

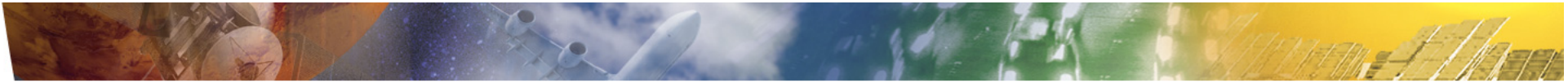
# **Current Activities in Numerical Unsteady Aerodynamics for Flutter- and Loads Analysis of Transport Aircraft**

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**DLR Institute of Aeroelasticity, Göttingen Germany**



Deutsches Zentrum  
für Luft- und Raumfahrt e.V.  
in der Helmholtz-Gemeinschaft



# Contents

- Overview of Unsteady Aerodynamics
- CFD Simulation of flutter, dynamic response and buffet
- Requirements of an efficient flutter analysis
- Methods for reduction of computational effort
  - Correction method
  - Transfer function method
  - Linearised CFD
  - POD Methods
- Conclusion

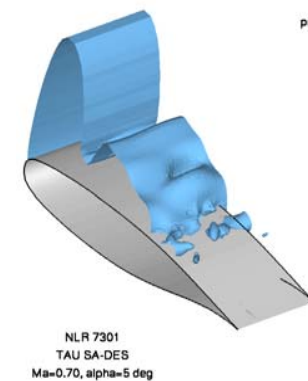
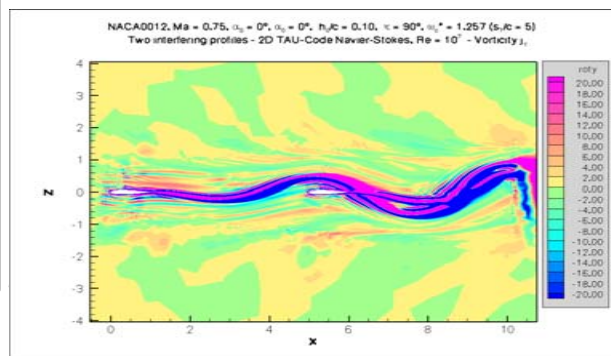
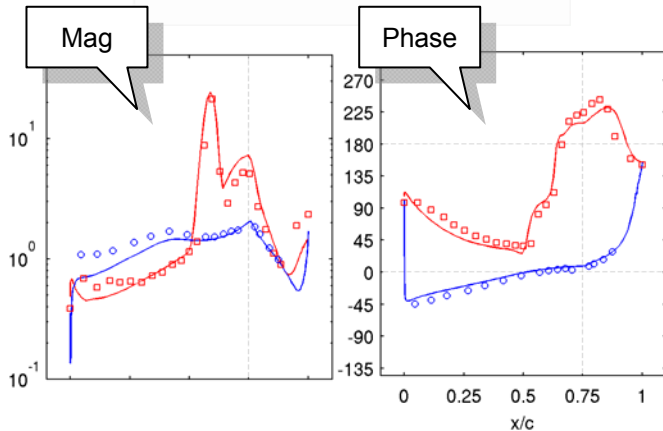
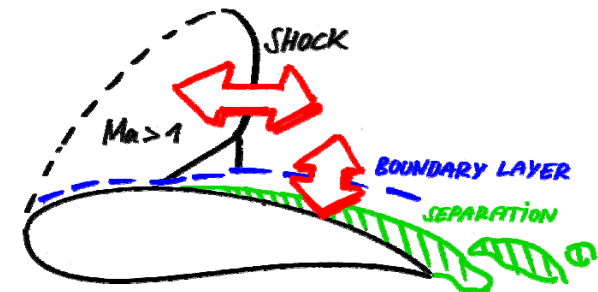
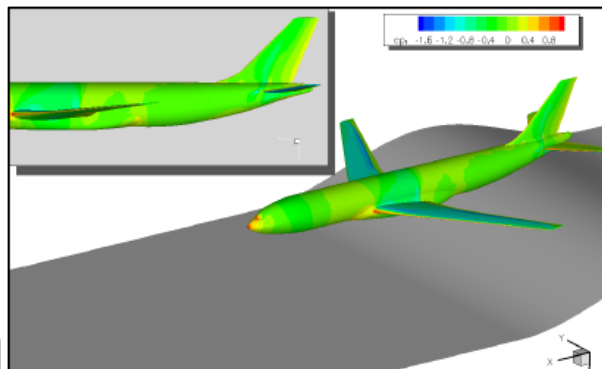
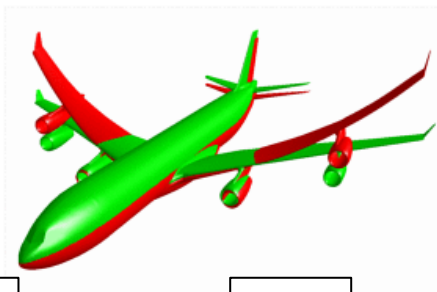
# Overview: Types of Unsteady Aerodynamic Problems

unsteady  
airloads

Motion-induced  
(Flutter)

Dynamic response  
(wakes, gusts)

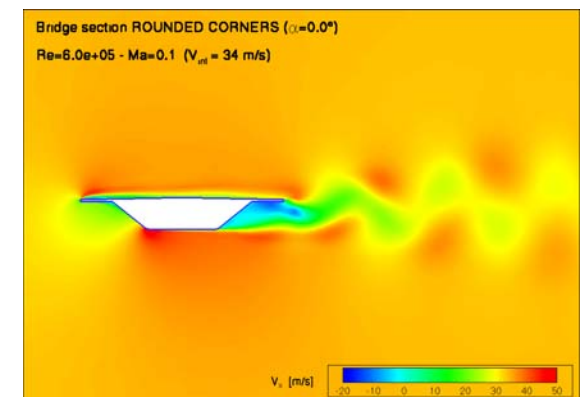
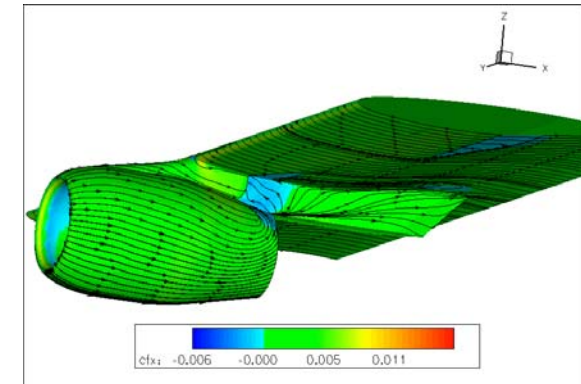
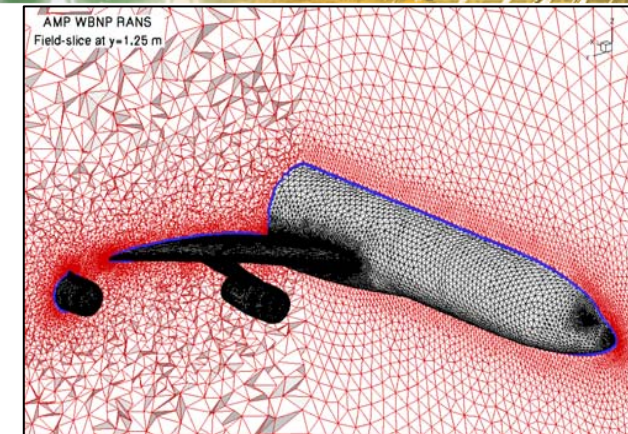
Flow-induced  
(separation, buffet)

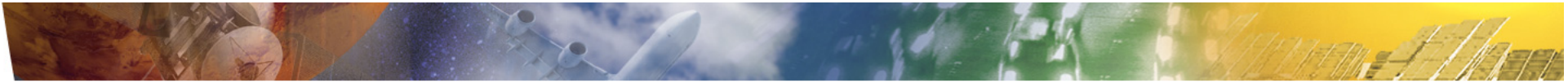




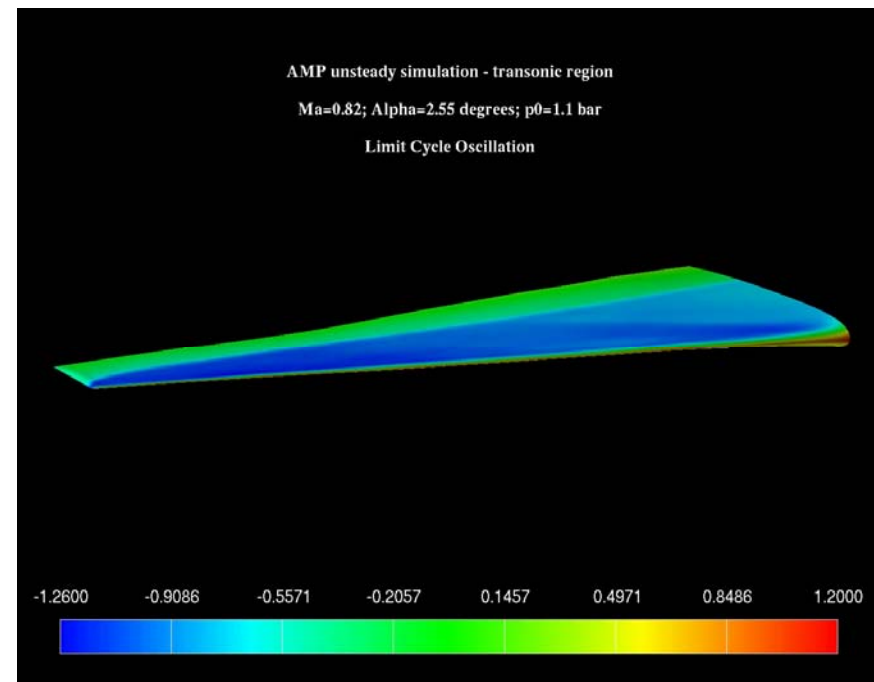
## Main Tool: DLR's TAU-Code

- 3D Finite Volume Scheme on unstructured hybrid grids (tetrahedra, prisms, pyramids, hexahedra),
- Integration of RANS- or Euler Equations
- 1-eq. , 2-eq- and RSM-turbulence models, DES
- Central or Upwind Spatial discretisation
- Time Integration by Explicit Multi-Step Runge-Kutta Scheme.
- Time Accuracy by Dual Time Stepping with Residual Smoothing for each Physical Time Step
- Local mesh adaptation: refinement/coarsening
- Chimera technique for overlapping grids
- High performance on parallel computers
- Efficient and robust Grid deformation tool
- Python-based fluid structure coupling





# CFD Flutter Simulation

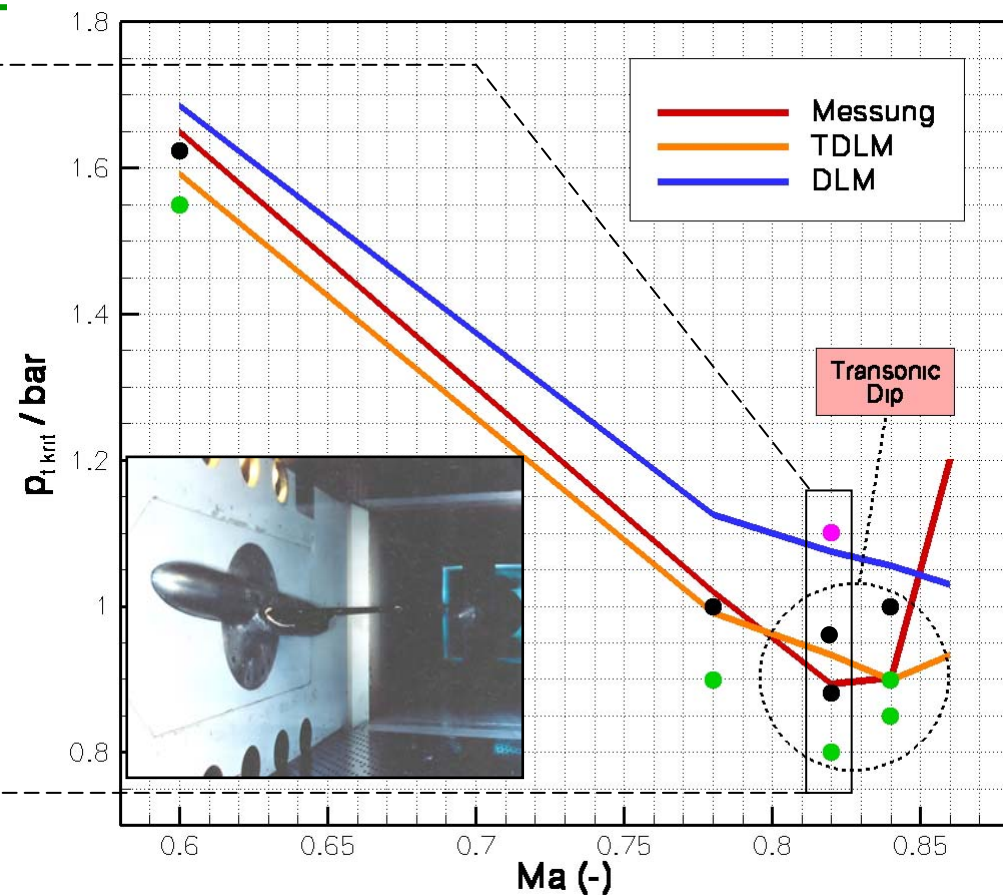
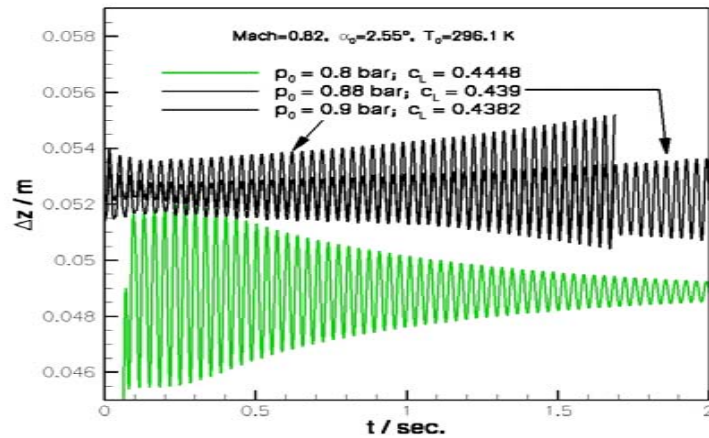
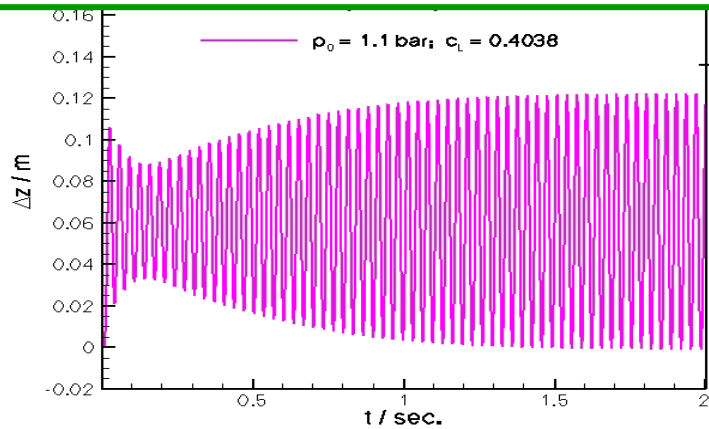


# CFD Flutter Simulation

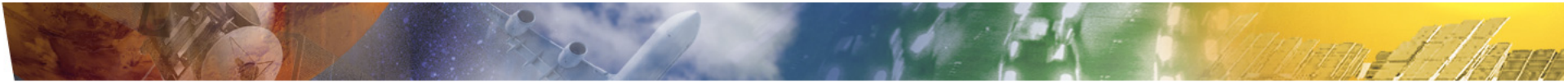
TAU-URANS – FEM coupling in time domain

Eigenvalue problem in frequency domain TDLM-Aerodynamics

$$[M]\{\ddot{u}\} + [D]\{\dot{u}\} + [K]\{u\} = \{f_a(u, \dot{u})\} = \text{aero}(-\omega^2 [\bar{M}] + [\bar{K}] - q_\infty [Q])\{\hat{q}_e\} = 0$$

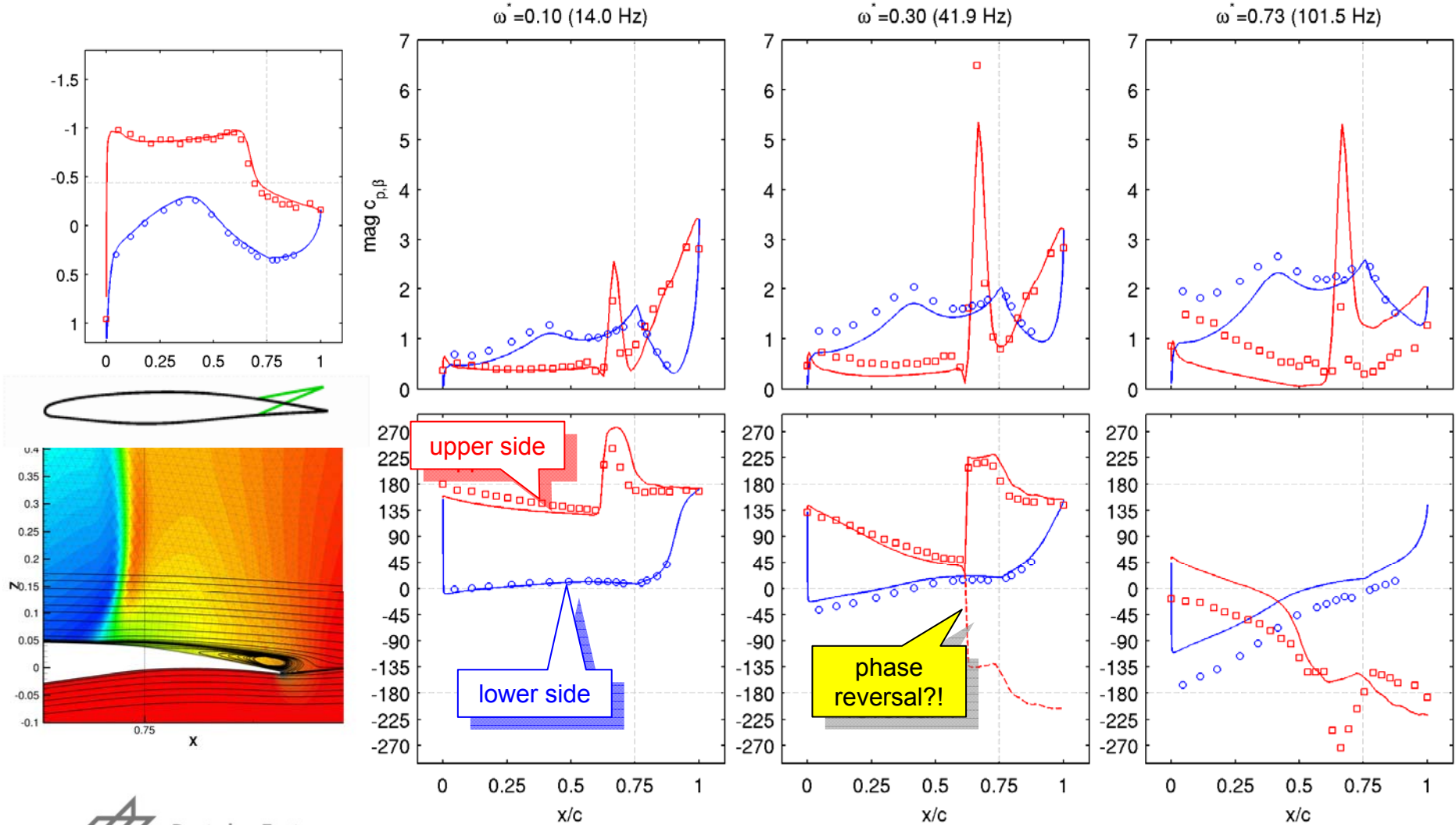




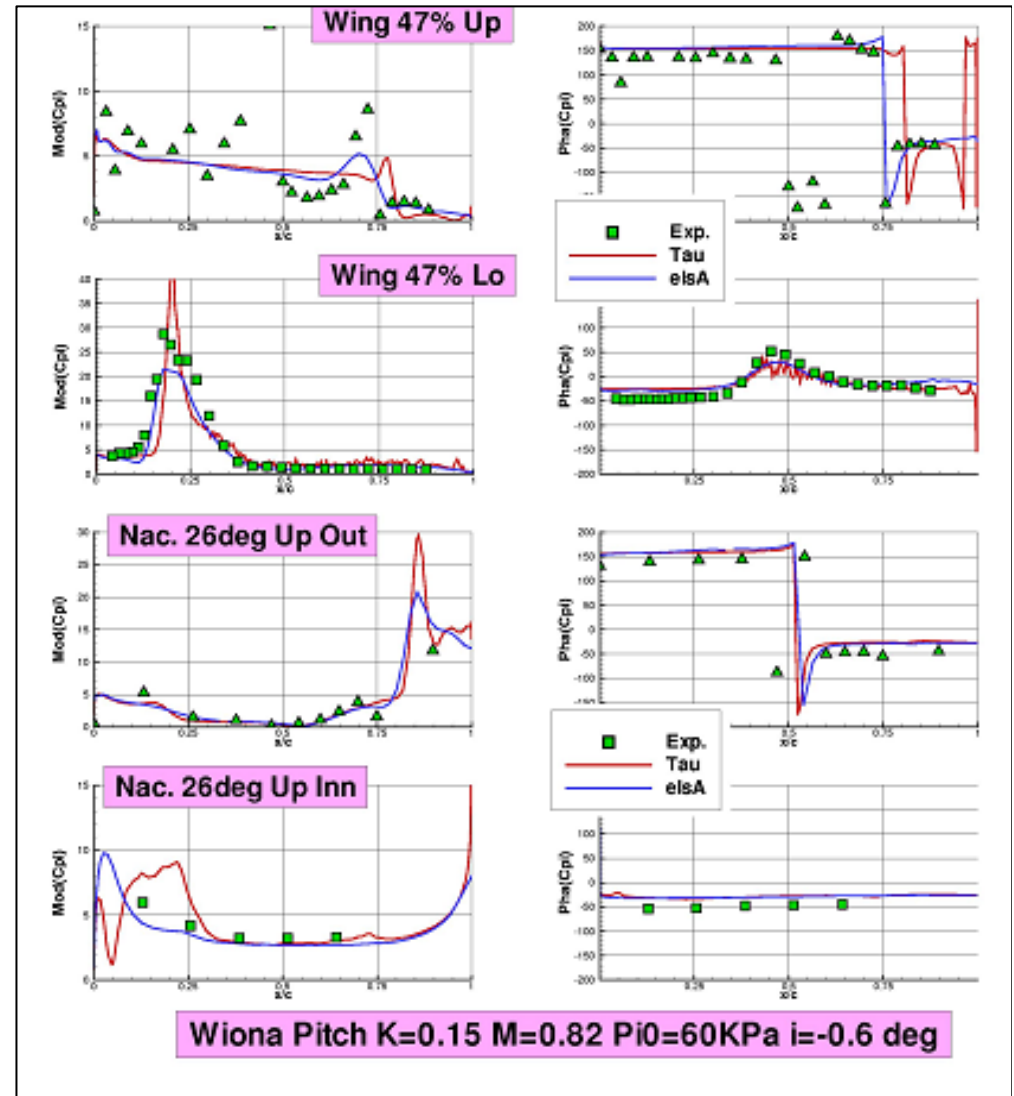
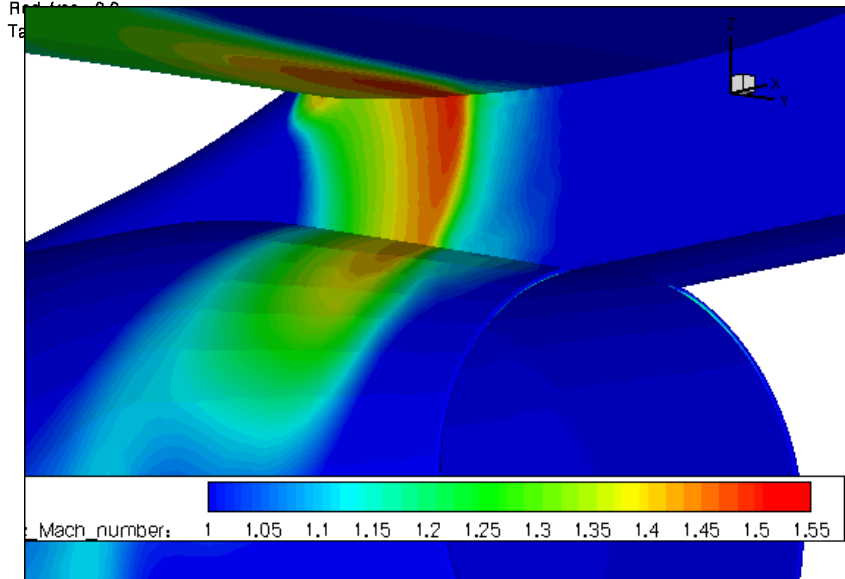
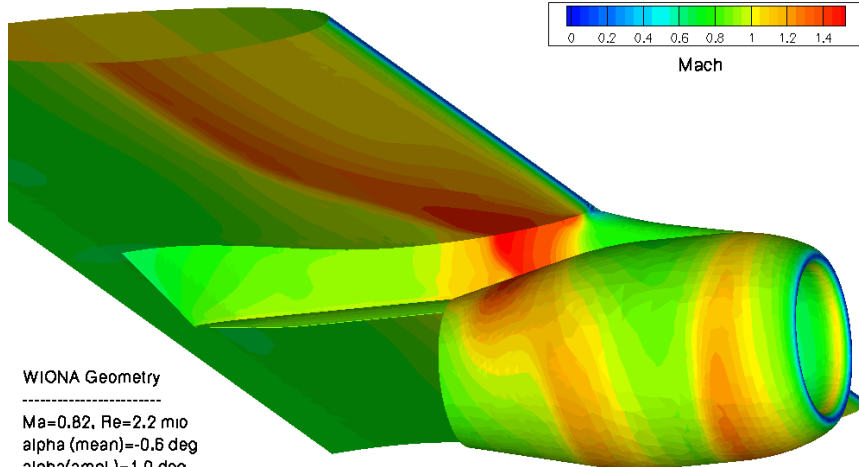


# Validation: Unsteady Control Surface Aerodynamics

Shock and flow separation close to hinge axis,  $Ma=0.80$ ,  $\alpha_0=2^\circ$ ,  $\beta_0=2^\circ$



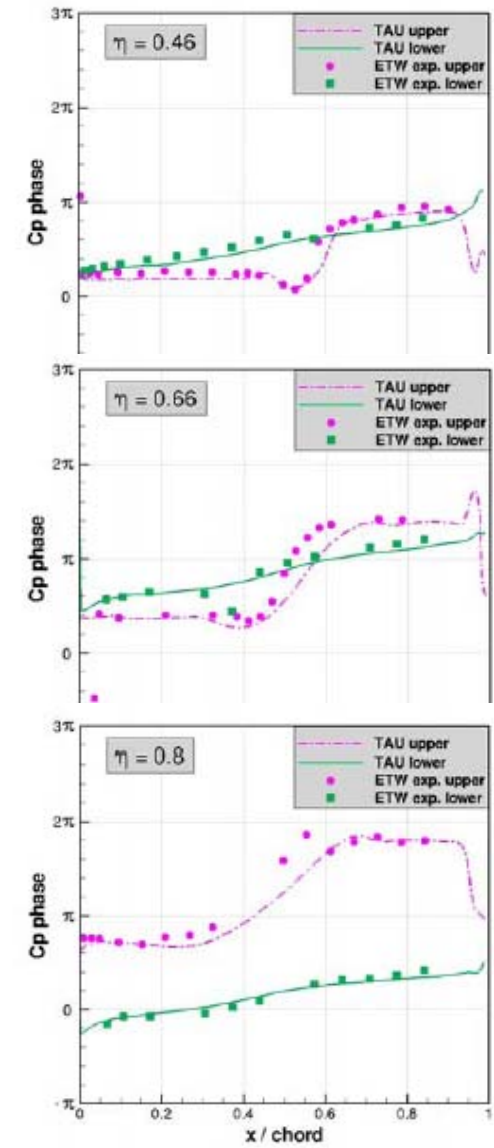
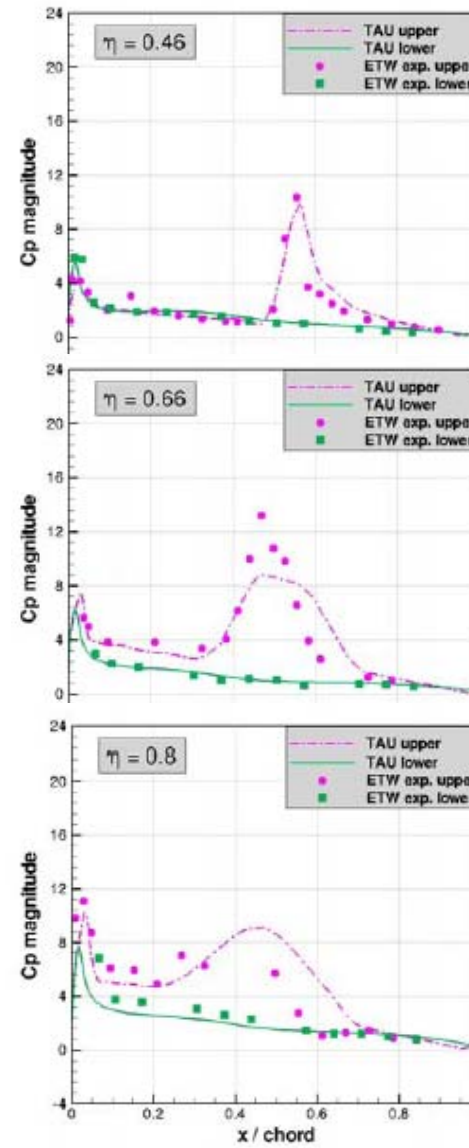
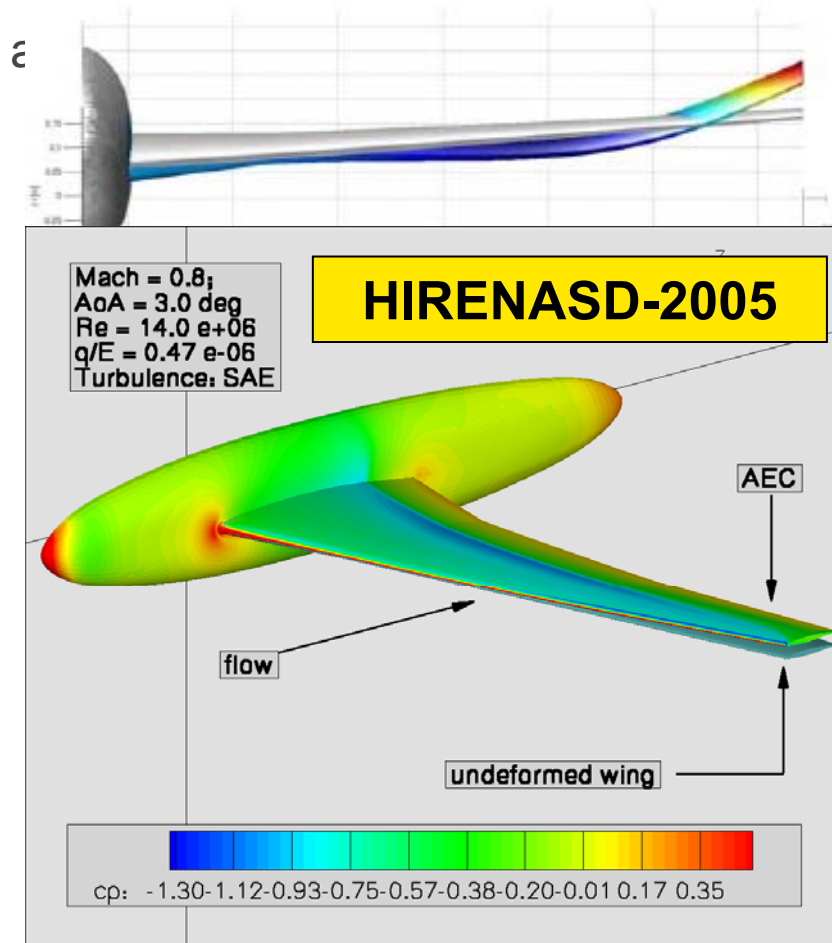
# Validation: Wing-Pylon-Nacelle Interference (WIONA)





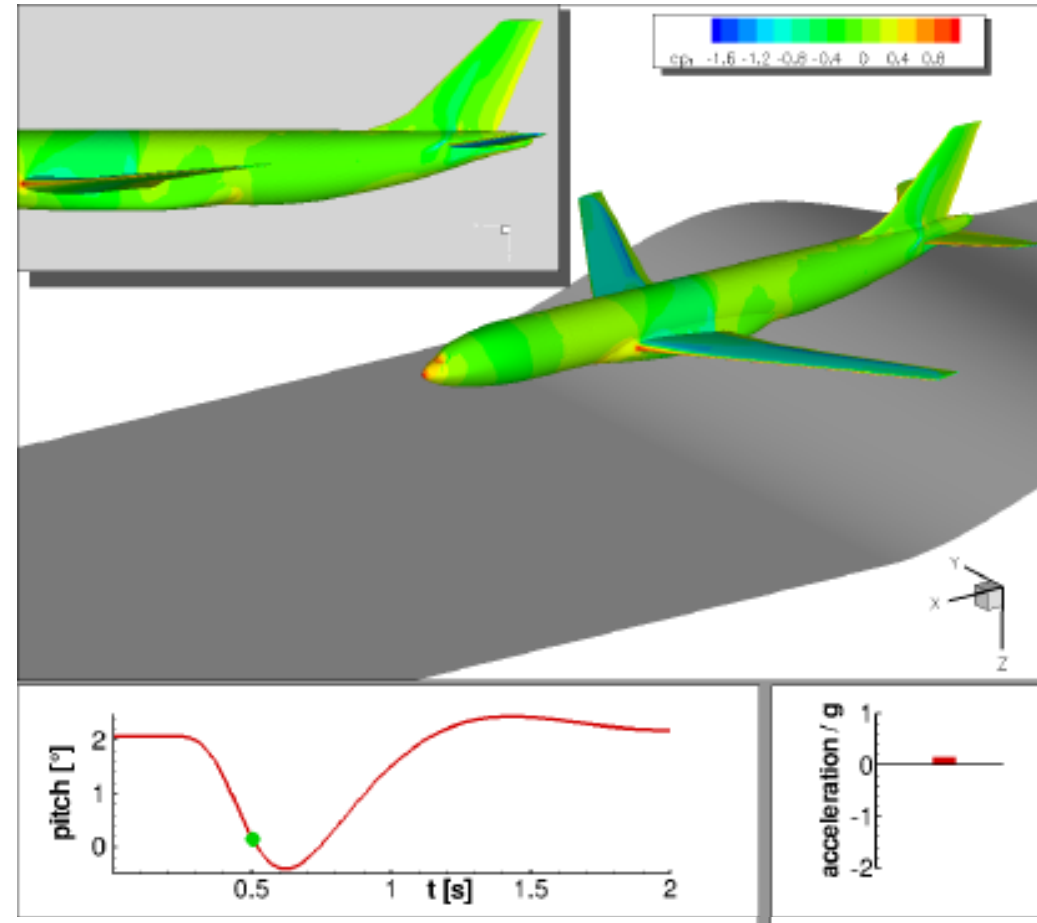
# Validation HIRENASD

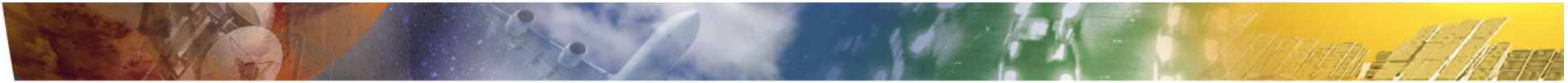
second mode shape,  $k=0.66$ , max. amplitude= $3.9e-3$  Ma=0.8, Re= $7e6$ ,



# High End Nonlinear Gust Analysis with TAU

- Gust amplitude = 30 m/s, Wavelength = 60 m
- $Ma = 0.85$ ,  $h = 11$  km,  $Re = 72 \times 10^6$
- Step 1: Trim steady horizontal flight
- Step 2: Coupling TAU with 6 flight mechanics DOFs
- Enforcement of  $(1 - \cos)$ -gust velocities at far field and in field
- Source: R, Heinrich, DLR-AS

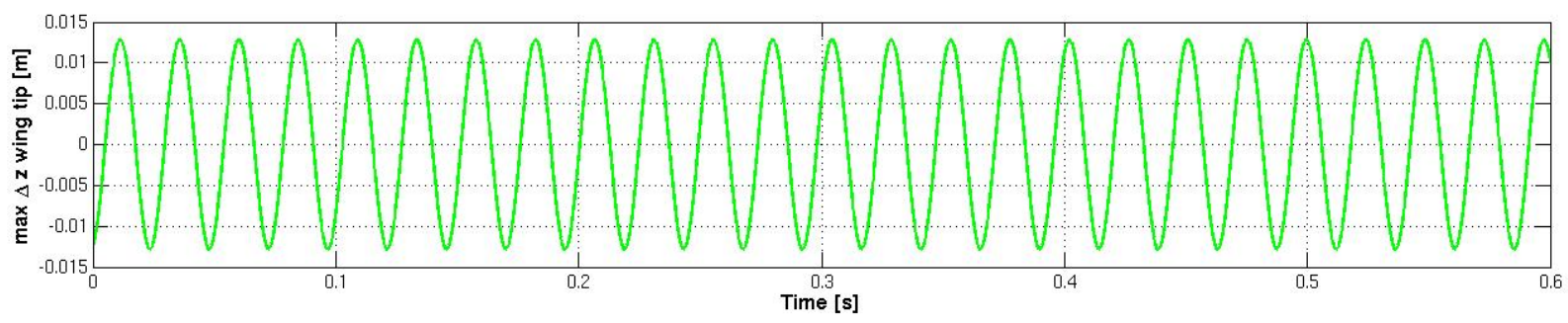
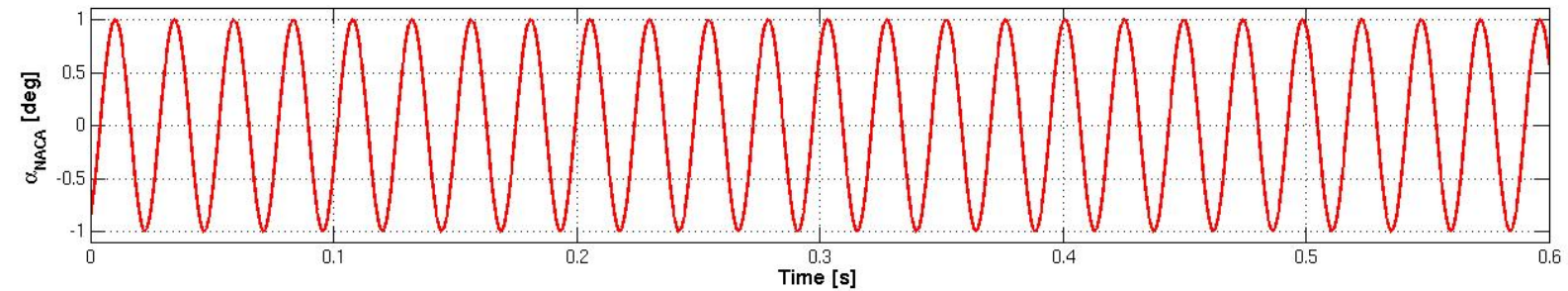
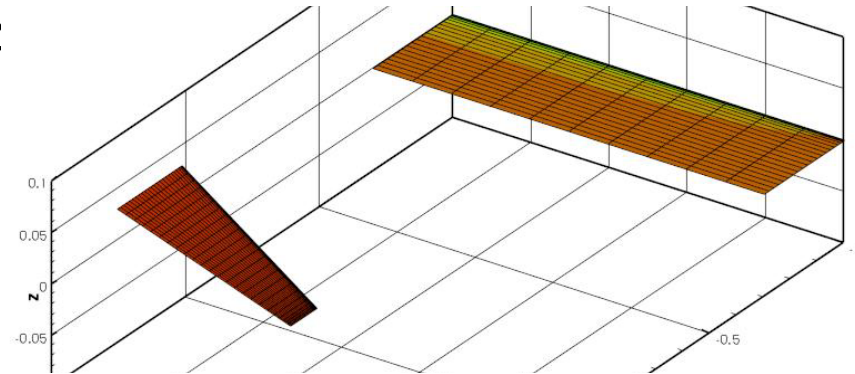




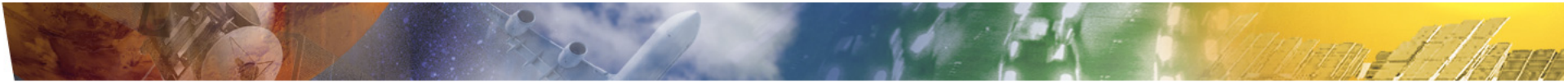
# Linear Loads- and Gust Analysis:

- $Ma = 0,75; \omega^* = 2\pi f b / u = 0,30914$
- Doublet Lattice Aerodynamics

$$\begin{aligned} \{\Delta c_p\} &= [AIC] \cdot \{w_{ind}\} \\ w_{ind} &= \alpha \cdot (1 + i \cdot x \cdot \omega^* / b) \end{aligned}$$

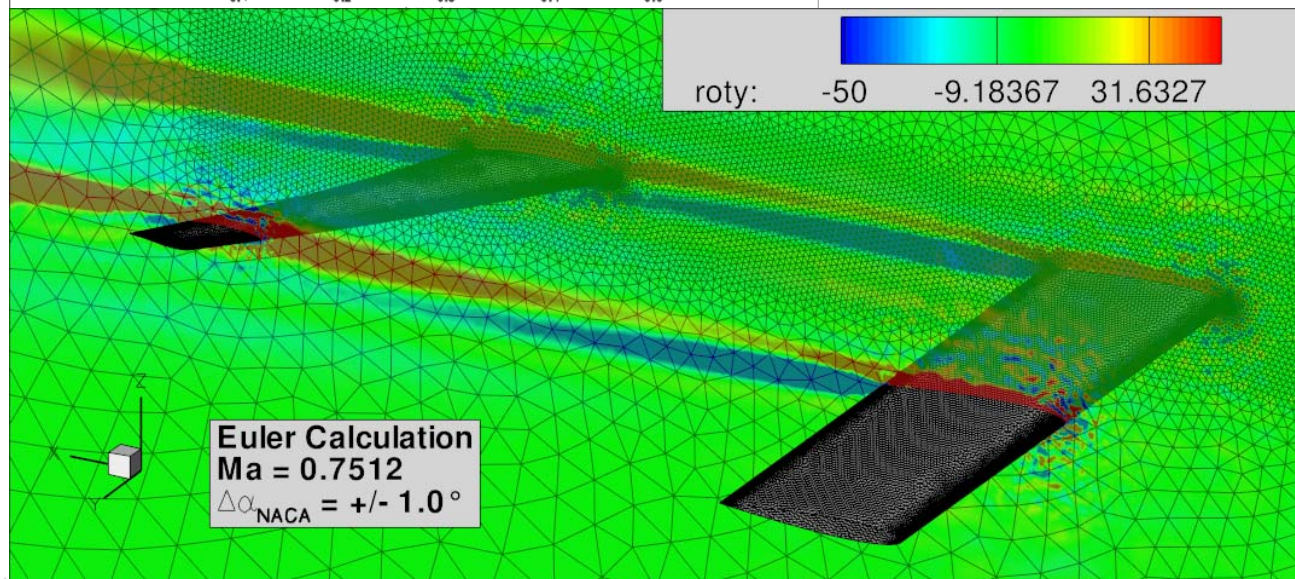
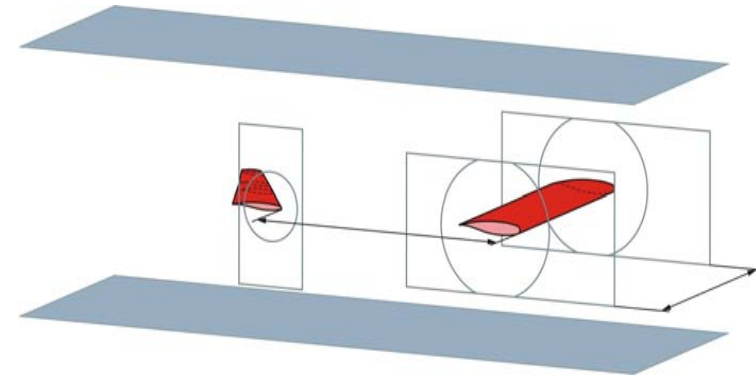
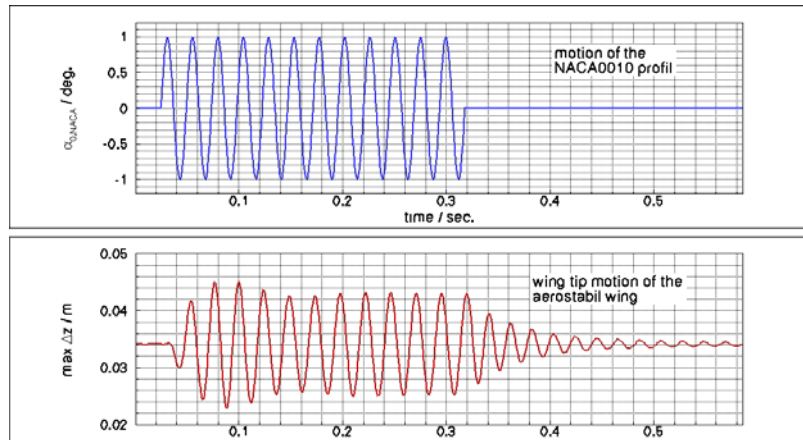




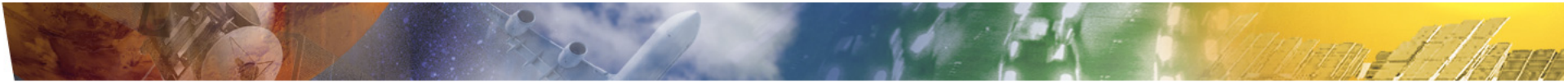


# Dynamic Response to Wake

## Windtunnel test – generic model for gust response





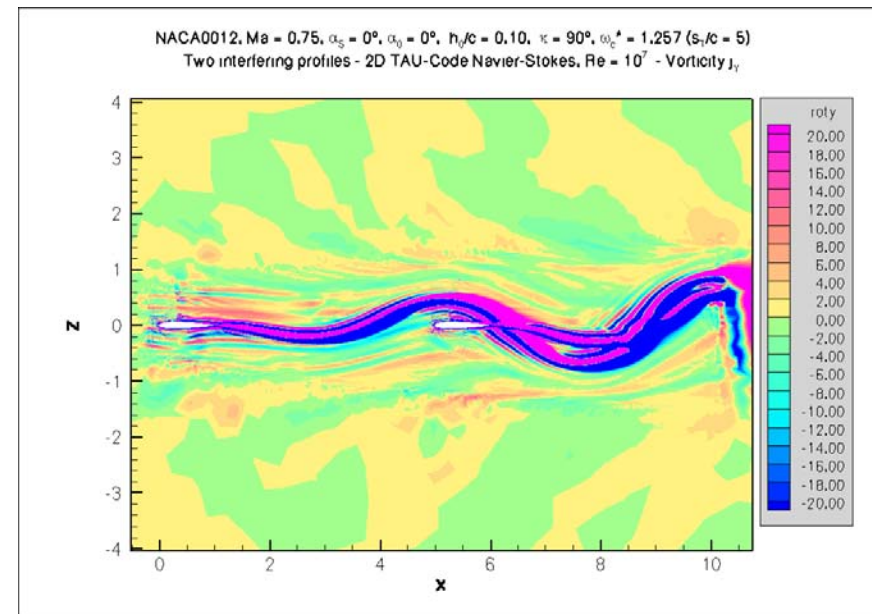
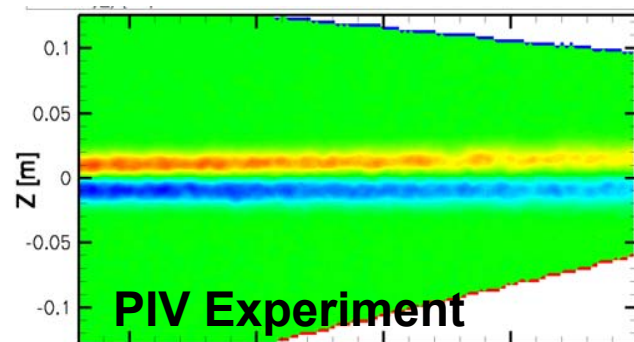
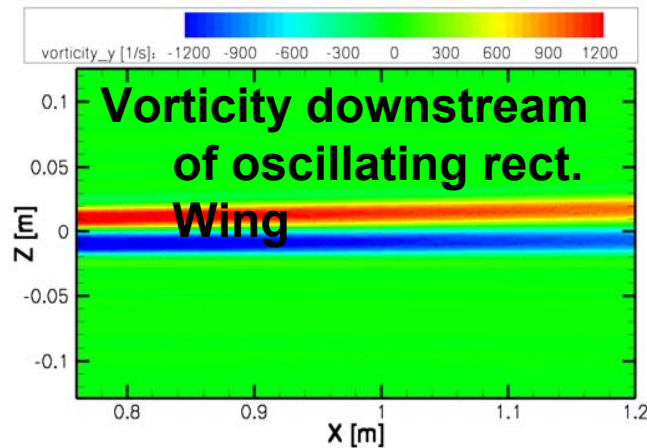
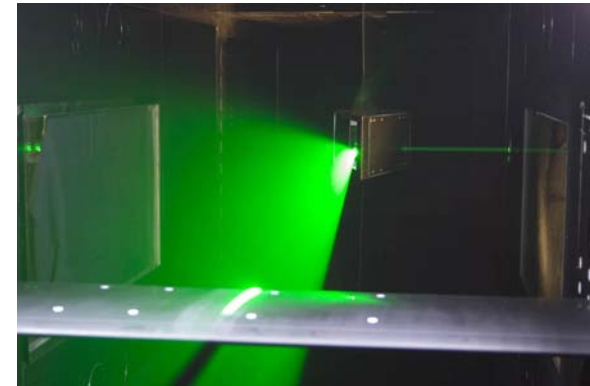


# Interference Problems

Atmospheric turbulence and gusts,

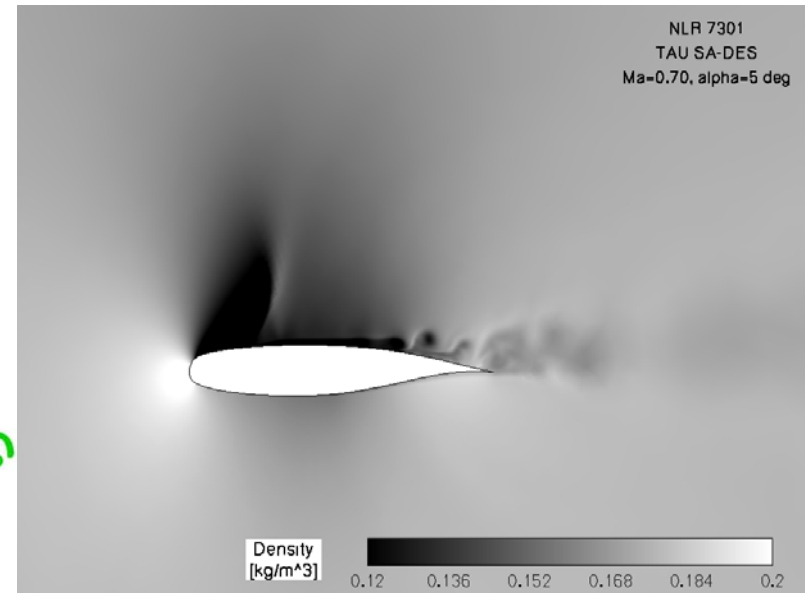
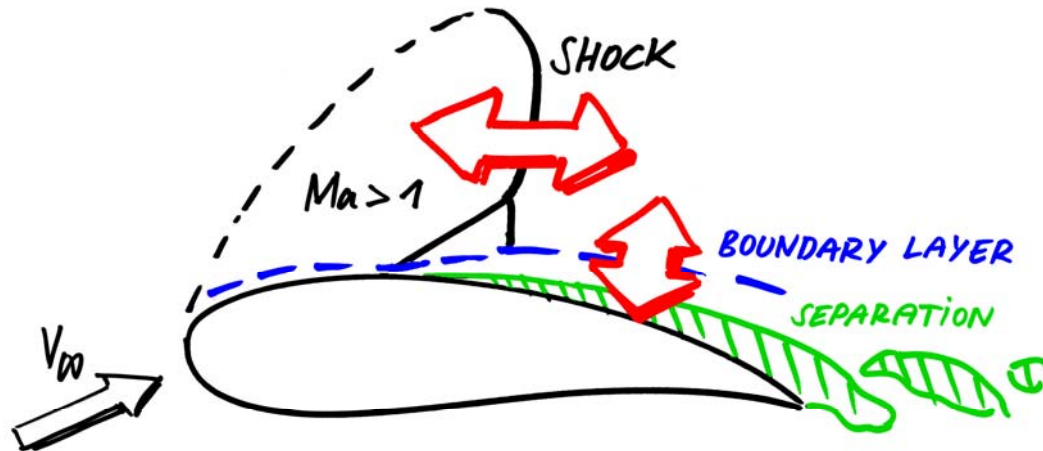
Wake and vortex interference

Numerical Simulations require fine grids for proper wake resolution



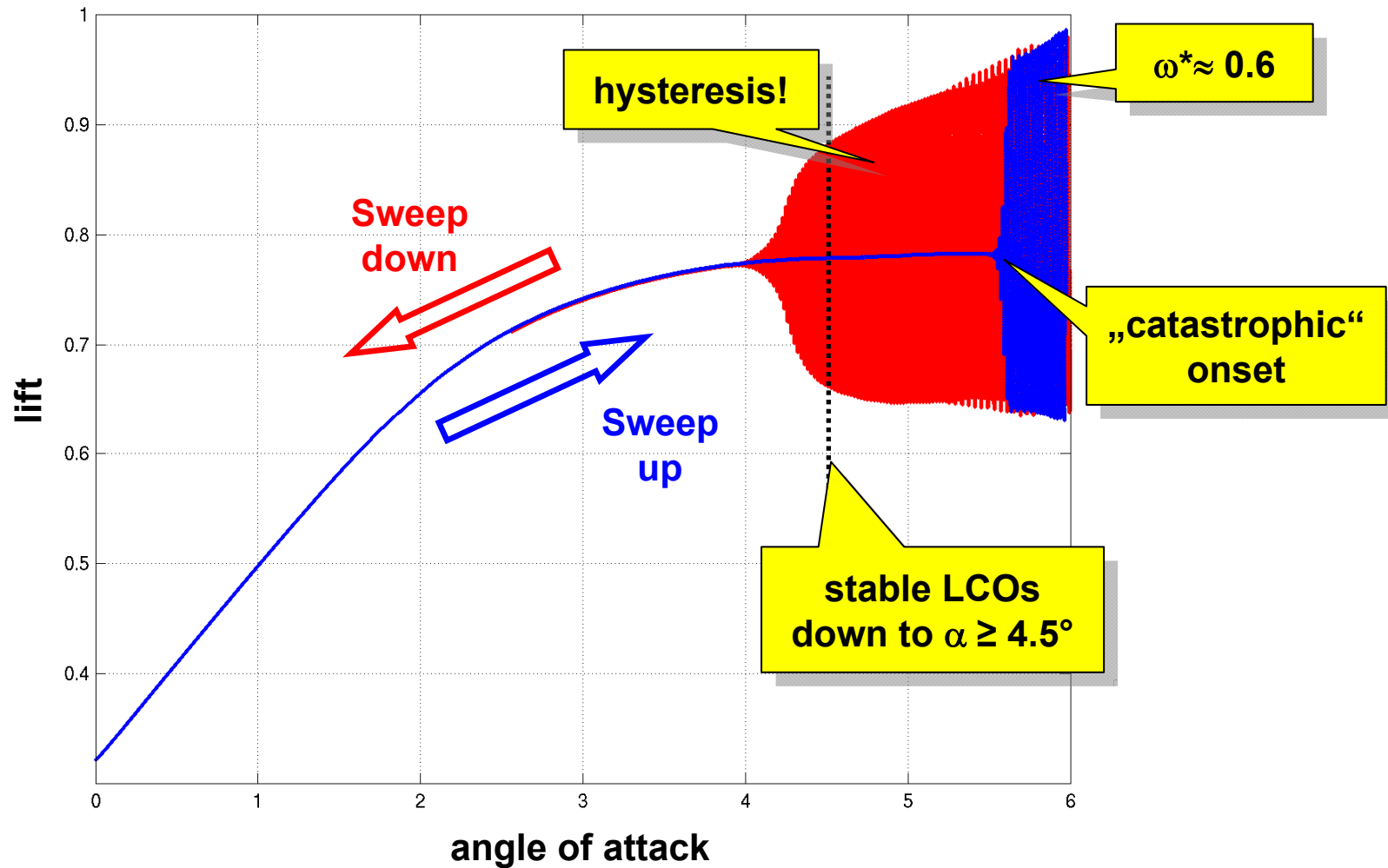
**TAU-Simulation: Vorticity for configuration of two oscillating airfoils**

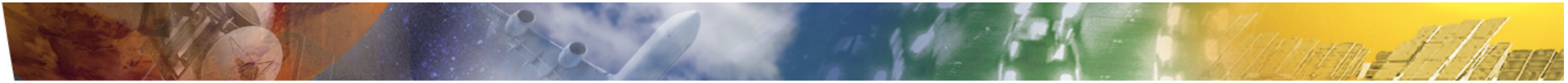
## The “shock buffet” phenomenon



- Pure aerodynamic, **self-excited shock oscillations** due to shock-boundary layer interaction in transonic flow
- Large-scale, low-frequency ( $Sr \approx 0.1$ ), beyond critical ( $Ma_{\infty}, \alpha$ )
- Fixed airfoil, i.e. **no elasticity** here
- Heavy loads, may couple with structural dynamics (“buffeting”)
- Can be simulated with CFD (qualitatively)
- **Physics of feedback mechanism still subject of discussion!**

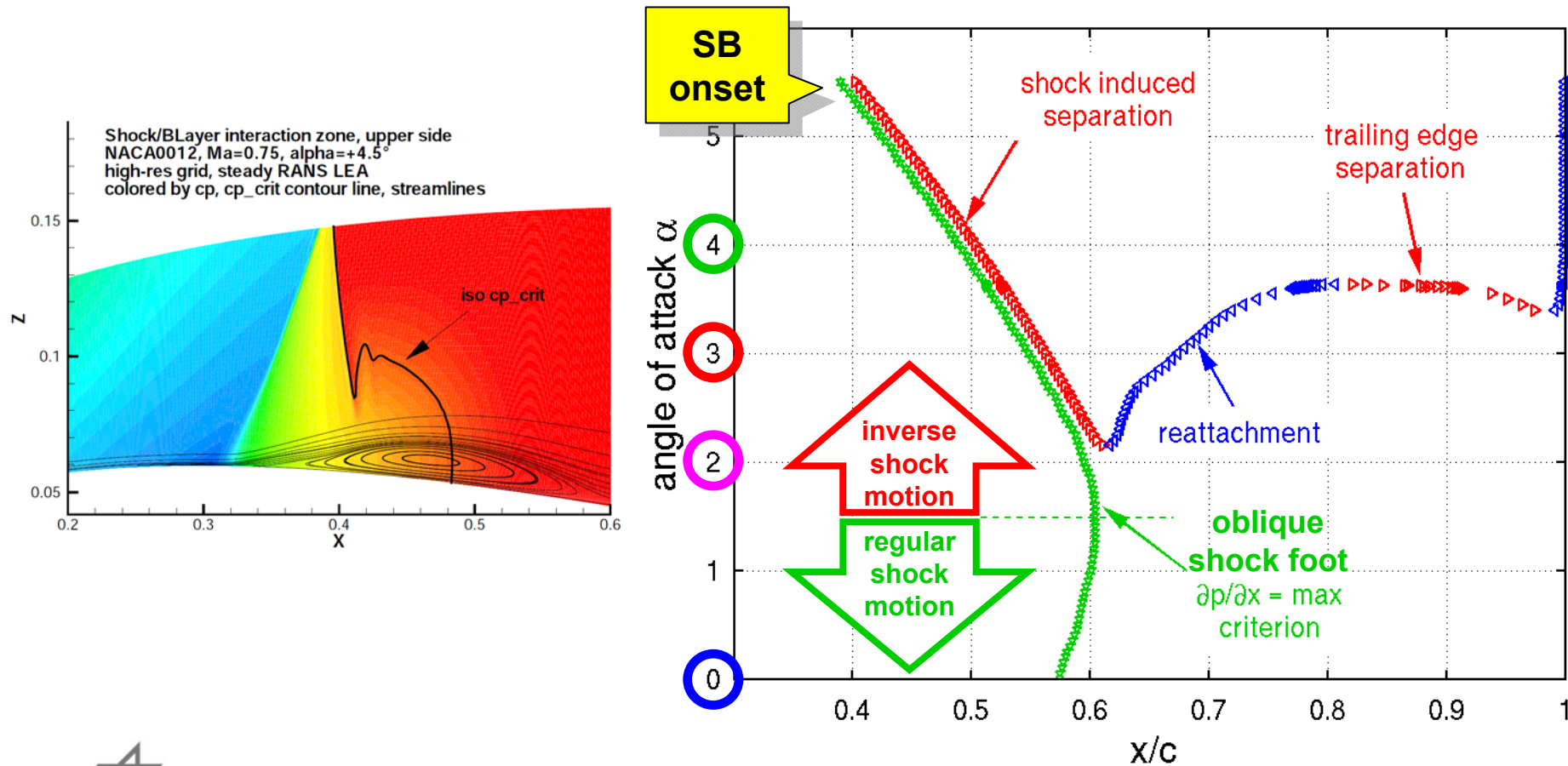
# Shock Buffet - direct simulation



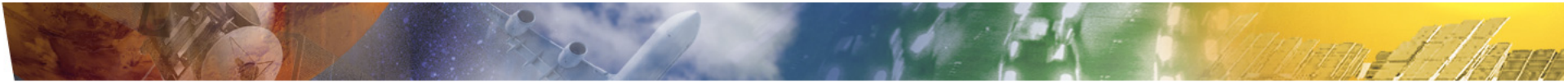


# Shock Buffet - Four subcritical mean flow fields

- Four different stable 2-d RANS flow fields around a supercritical airfoil at  $Ma=0.75$  and  $\alpha_0 = 0^\circ, 2^\circ, 3^\circ, 4^\circ$  :



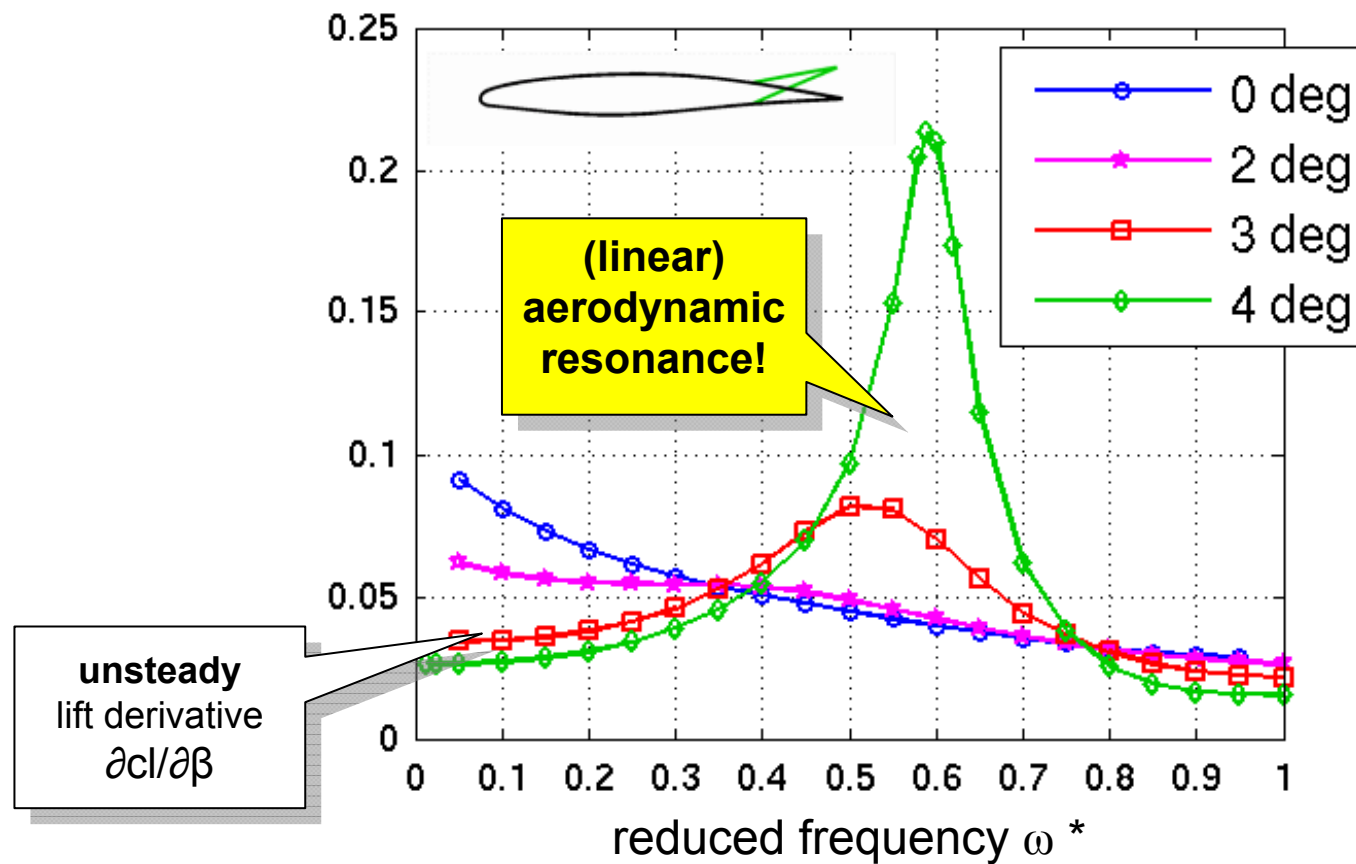




# Shock Buffet

## Subcritical frequency response

- Excitation of the flow with **(very!) small, harmonic perturbations** in the time domain (arbitrary kinematics)



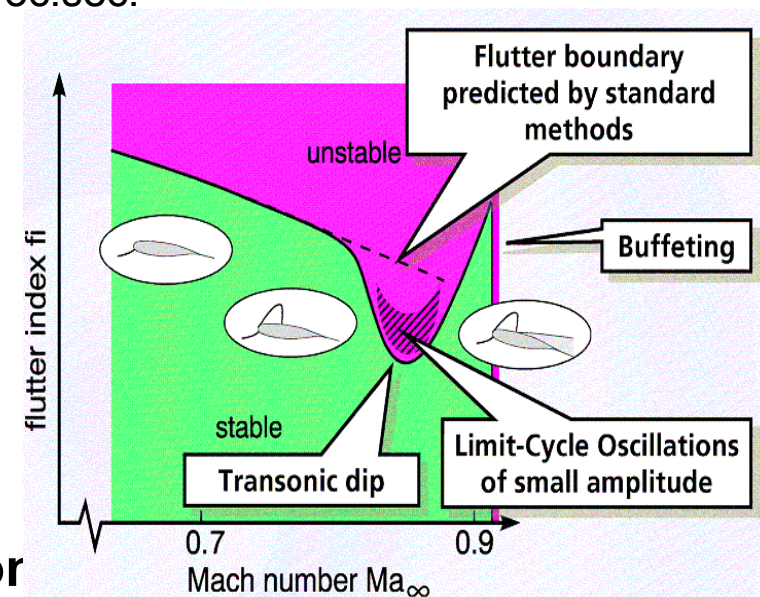
# Efficiency Improvement of Flutter Analysis in transonic and separated flow

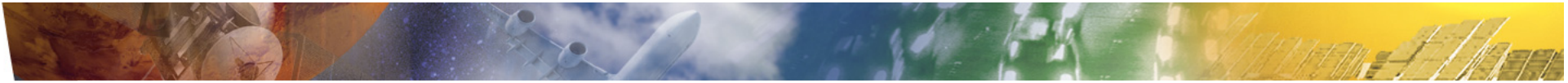
Flutter analysis of an aircraft needs computations for many parameter combinations:

- Mach numbers: 1-7, Frequencies: 5-12, Symmetric-Antidymmetric: 2, Modes: 40-150,
- Payload/fuel weight: 15-20, trimmed (elastic) flight condition: 1-3 → > 1 Mio!
- CFD effort for example TAU-URANS, CFD Half model, 5.417 Mio grid cells
- 27 h CPU per single case (32 Prozessors) = 3 Mio Proc.sec!

→ **Reduktion of CFD effort necessary**

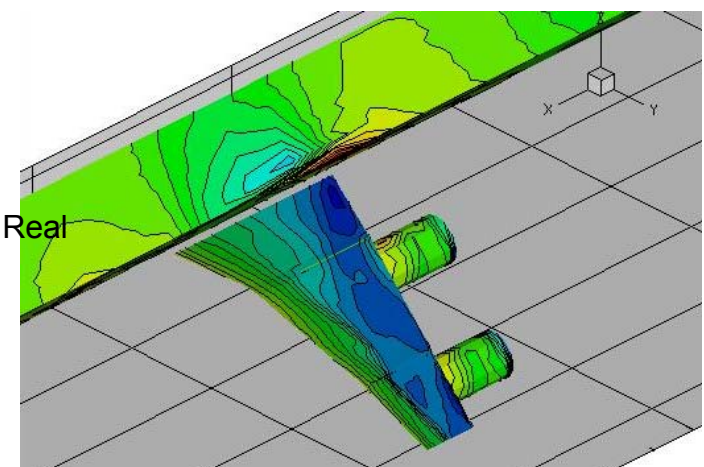
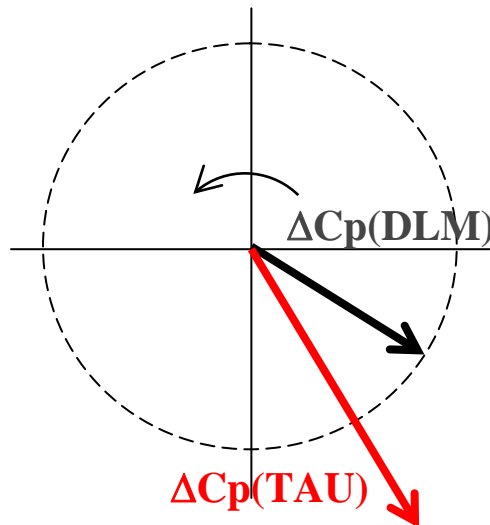
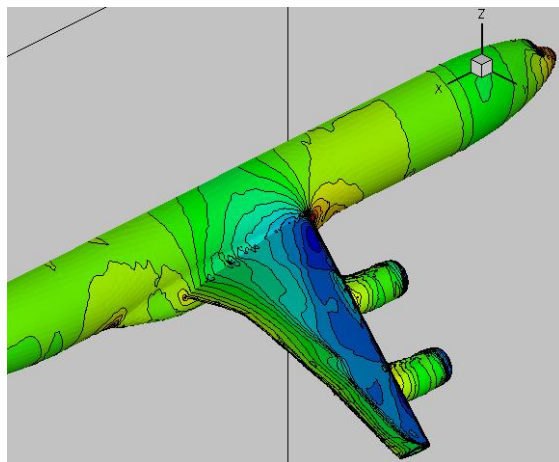
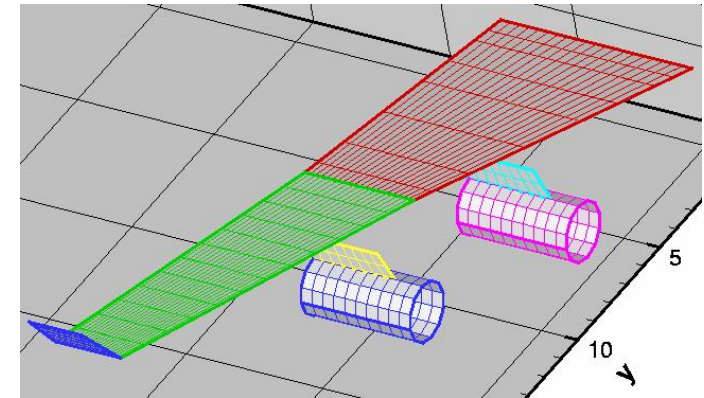
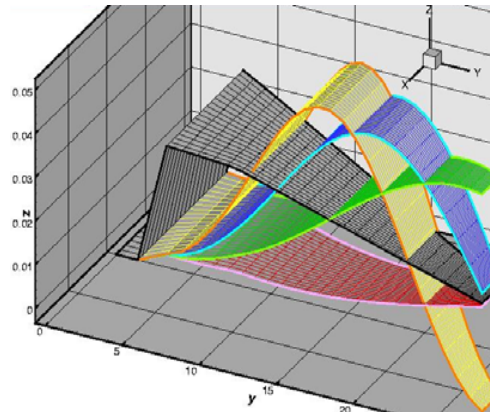
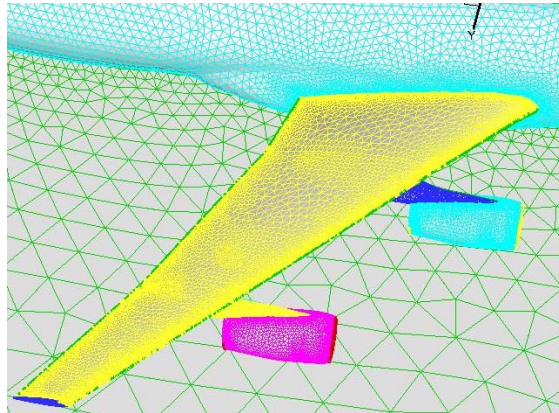
- **Correction of classical subsonic DLM**
- **Transfer Functions**
- **Application of less sophisticated CFD (Euler+boundary-layer)**
- **Linearised CFD**
- **POD (Proper Orthogonal Decompositor**





# CFD4Flutter – RANS based CFD-Correction of DLM

Complete CFD Simulation → for selected Basic modes → correction of DLM Aero

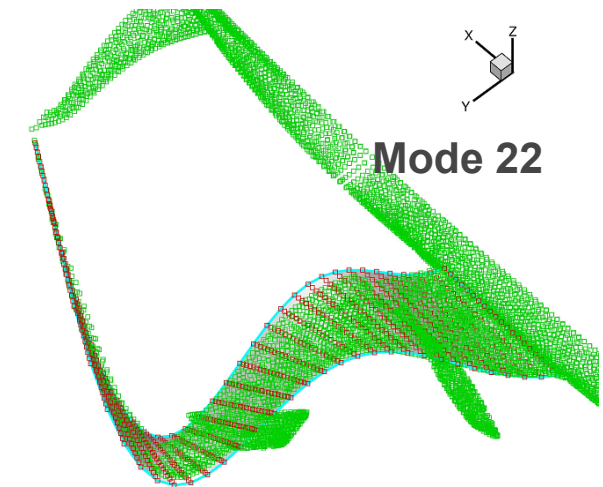
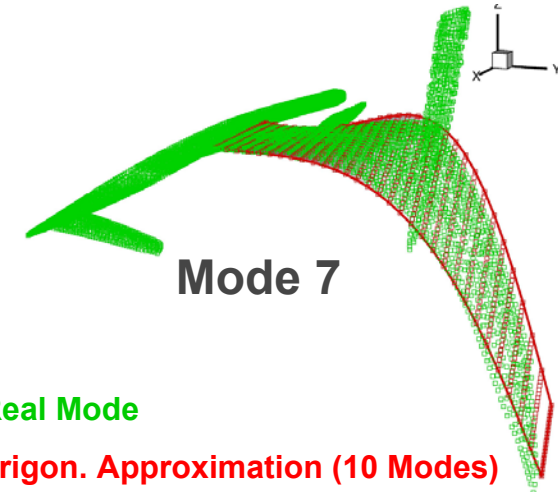
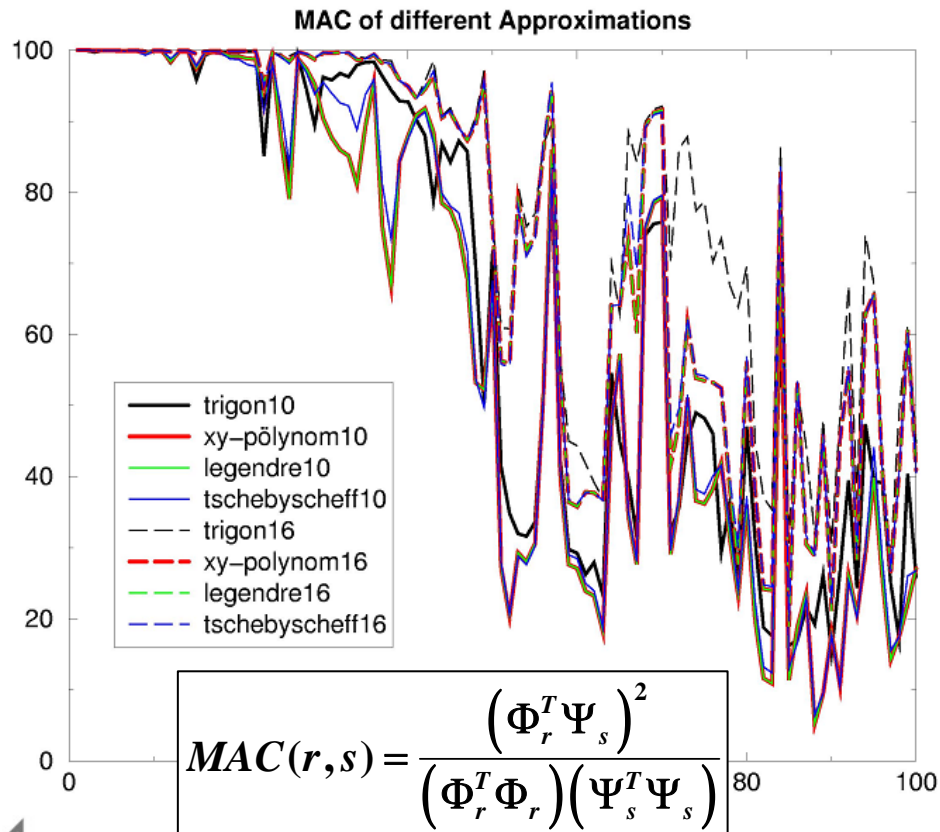




# Approximation of Elastic Modes

- 10 synthetic modes sufficient for approximation of first 50 real aircraft modes (MAC values > 80%).
- Trigonometric approach for synthetic modes

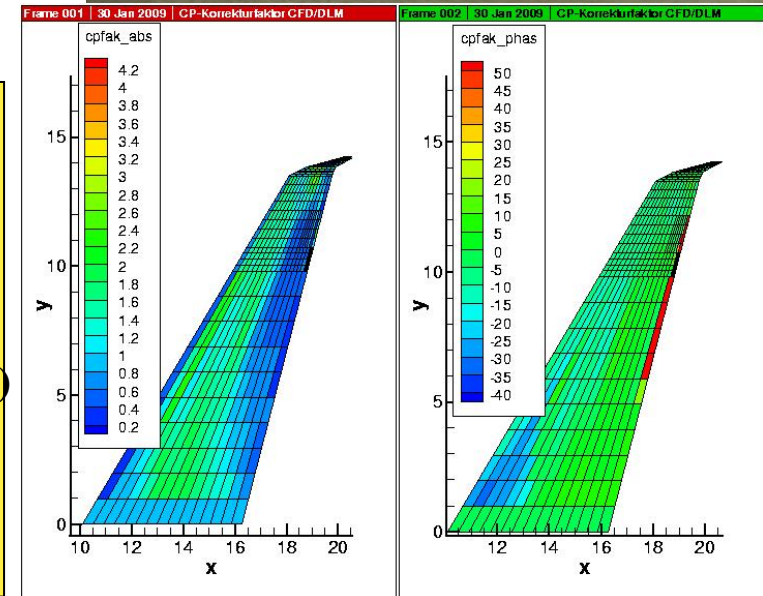
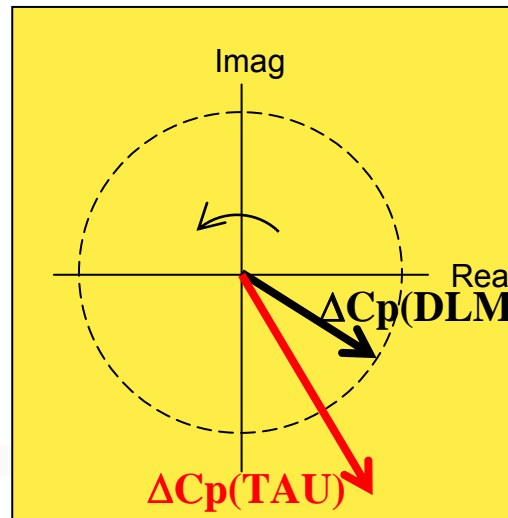
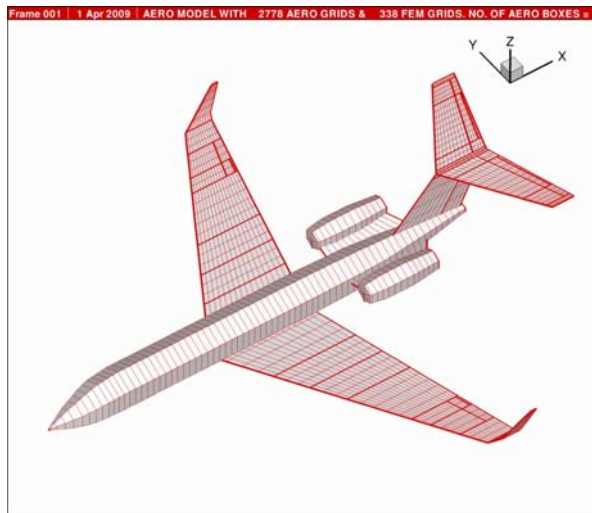
First 100 A340-300 Eigen Modes





# Application to DLR Research Aircraft G550-HALO

- CFD half model, RANS, 5.417 Mio cells,
- Unsteady aero data base for forced oscillations of trimmed aircraft in static aeroelastic equilibrium
- 300 cases (3 Ma, 2 cl, 5  $\omega^*$ , 10 synth. modes)
- Flutter computation based on unsteady aerodynamic corrected data, 95 modes from Ground Vibration Test



Correction factor (magnitude and phase)

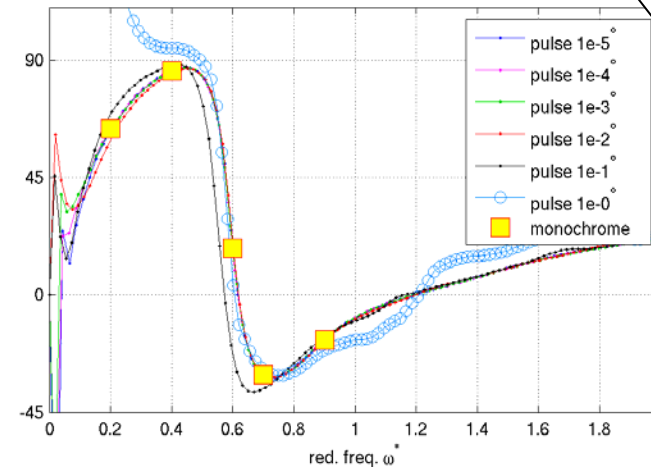
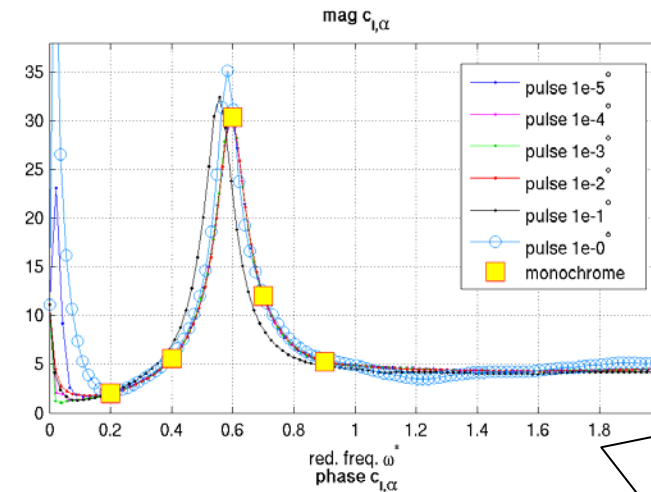
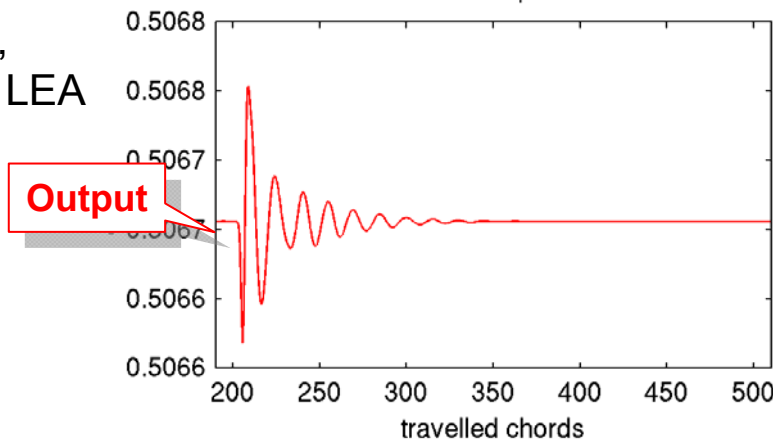
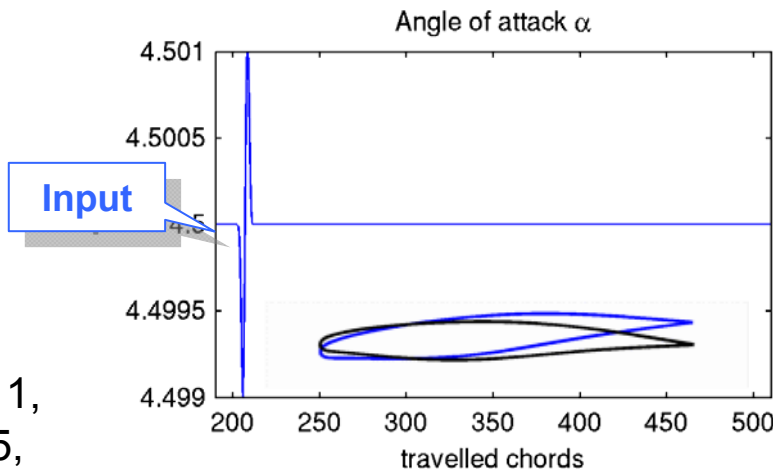
(1. Torsion, Ma=0.8, k=0.25)

# Transfer Functions – Impulse Method

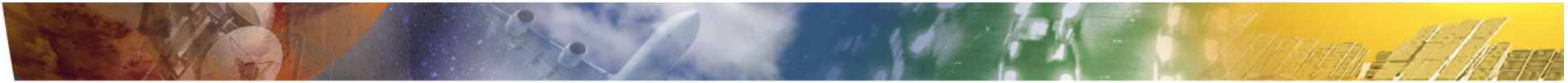
Unsteady 1. Harmonic of lift extracted from pulse excitation of airfoil.

Linearity of transonic and separated flow for small disturbances!

BAC 3-11,  
 Ma=0.75,  
 $\alpha_0=4.5^\circ$ ,  
 TAU 2D,  
 URANS LEA



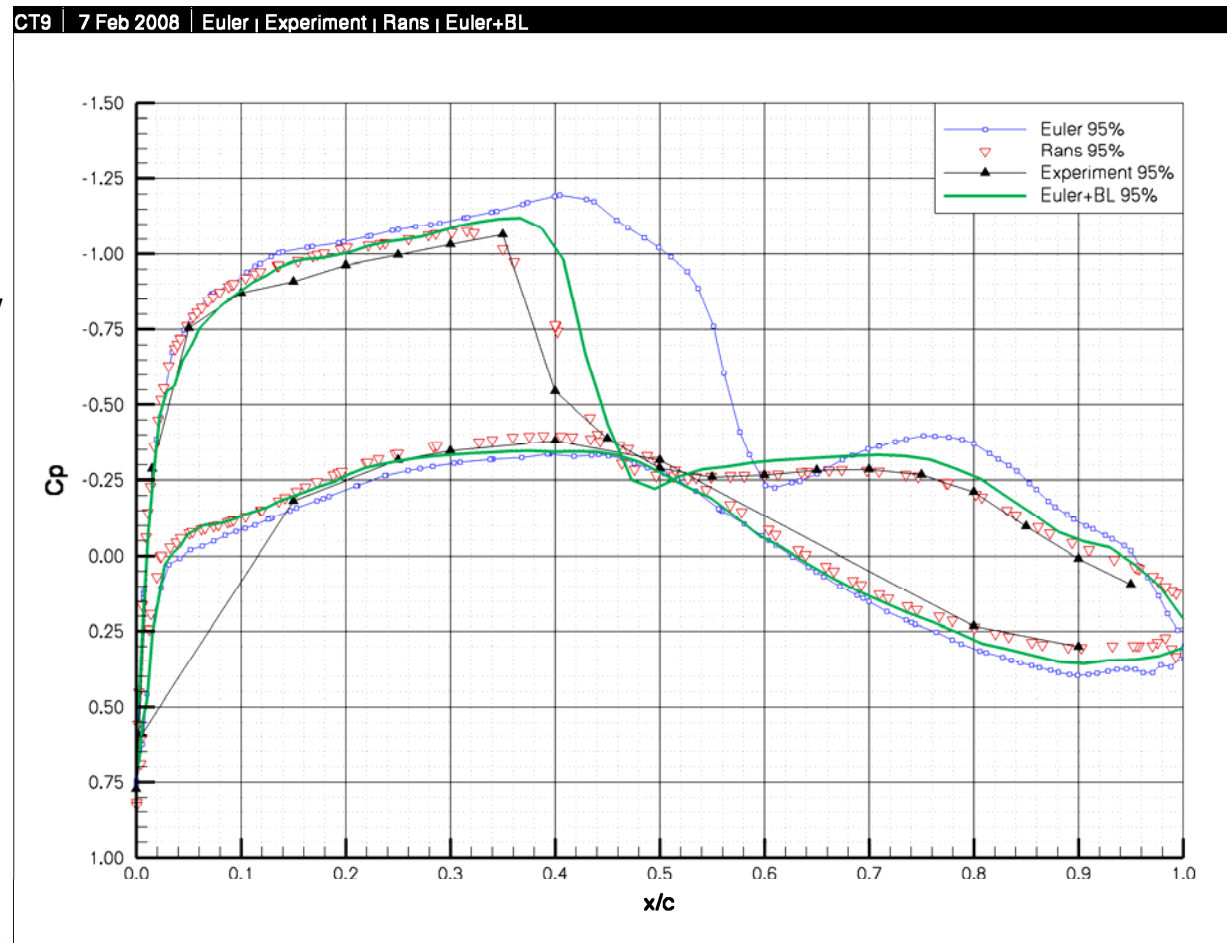
frequency-domain  
 Magnitude  
 of output  
 Scaled with  
 magnitude  
 of input

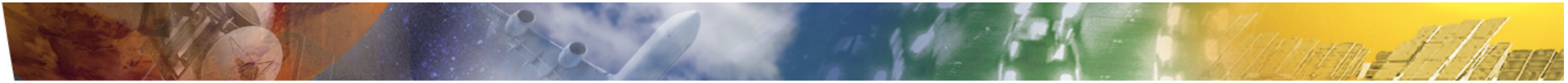


# Euler – Boundary layer Coupling

## Testcase LANN CT9 with shock-induced flow separation

- TAU with 2D inverse Integral Boundary Layer Method
- Carter Coupling
- For attached flow o.k.
- Not for separated flow





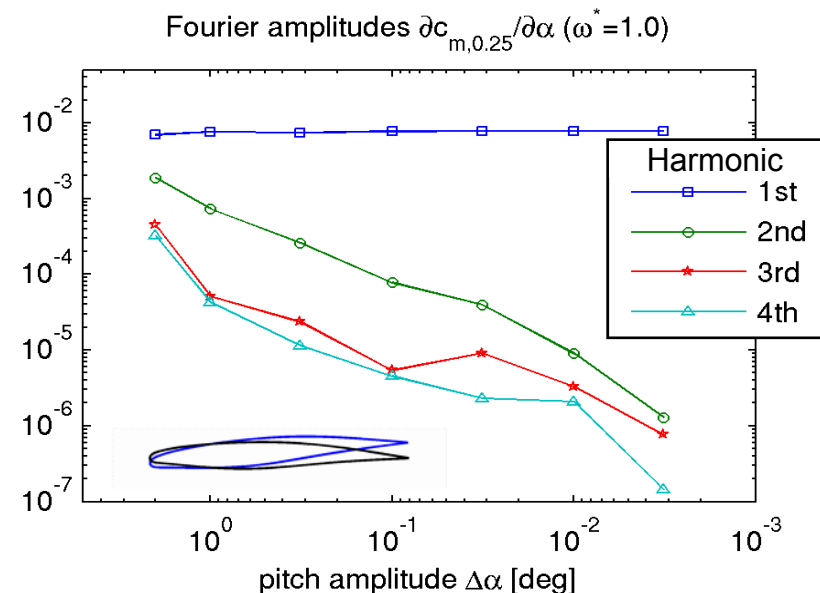
# Linearised CFD

## Justification

- Small perturbations of boundaries → small linear perturbations of (nonlinear) mean flow field
- Mean flow may comprise shock waves and flow separation
- Motion of shock waves or separation bubbles are nearly proportional to boundary perturbation
- This approximation is sufficient for aeroelastic stability analysis

## Difficulties and limits

- LCO (large shock motion or separation motion)
- Linearisation for separated flow difficult
- Linearisation of turbulence models?
- Linearisation of transition?





# Linearised Frequency Domain Solver (LFD)

➤ Unsteady RANS Equation (1):

$$\frac{du}{dt} + R(u, x, \dot{x}) = 0$$

➤ Fourier series expansion

$$u(t) = \bar{u} + \tilde{u}(t) = \bar{u} + \sum_k (\hat{u}_k e^{ik\omega t})$$

➤ of u(t) and x(t)

$$x(t) = \bar{x} + \tilde{x}(t) = \bar{x} + \sum_k (\hat{x}_k e^{ik\omega t})$$

➤ analysis of small periodic motions

➤ **Linearisation** of (1)

$$\frac{du}{dt} + \left. \frac{\partial R}{\partial u} \right|_{\bar{u}, \bar{x}} \tilde{u} + \left. \frac{\partial R}{\partial x} \right|_{\bar{u}, \bar{x}} \tilde{x} + \left. \frac{\partial R}{\partial \dot{x}} \right|_{\bar{u}, \bar{x}} \dot{\tilde{x}} = 0$$

➤ about steady equilibrium condition:

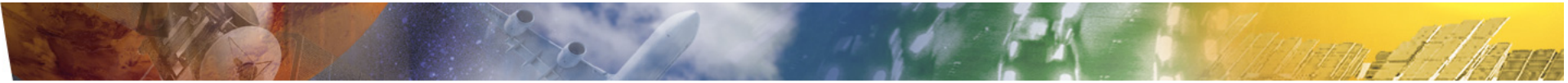
➤ Fourier expansion yields a complex valued linear system of equations

$$Ax = b$$

$$A = \begin{pmatrix} \frac{\partial R}{\partial u} & -k\omega I \\ k\omega I & \frac{\partial R}{\partial u} \end{pmatrix} \quad x = \begin{pmatrix} \hat{u}_{real} \\ \hat{u}_{imag} \end{pmatrix} \quad b = \begin{pmatrix} \frac{\partial R}{\partial x} \hat{x}_{real} + k\omega \frac{\partial R}{\partial \dot{x}} \hat{x}_{imag} \\ -\frac{\partial R}{\partial \dot{x}} \hat{x}_{imag} - k\omega \frac{\partial R}{\partial x} \hat{x}_{real} \end{pmatrix}$$

➤ b computed by:

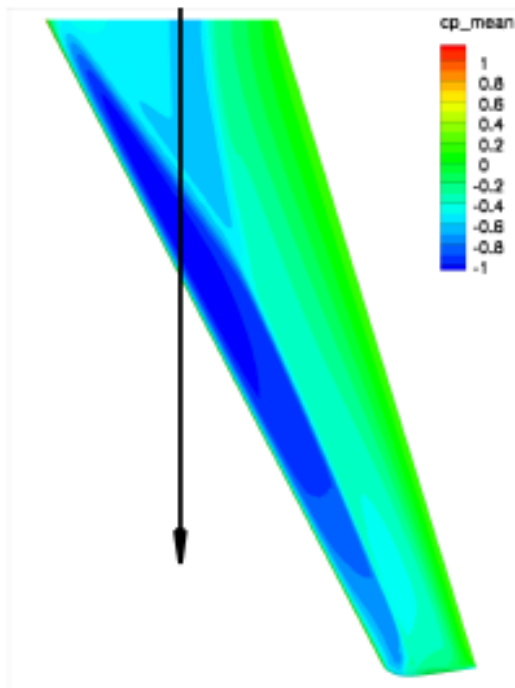
$$\frac{\partial R}{\partial x} \hat{x}_{real} = \frac{\Delta R(\bar{u}, \bar{x} \pm \epsilon \hat{x}, 0)}{2\epsilon} \quad \frac{\partial R}{\partial \dot{x}} \hat{x}_{imag} = \frac{\Delta R(\bar{u}, \bar{x}, \pm \epsilon \hat{x})}{2\epsilon}$$



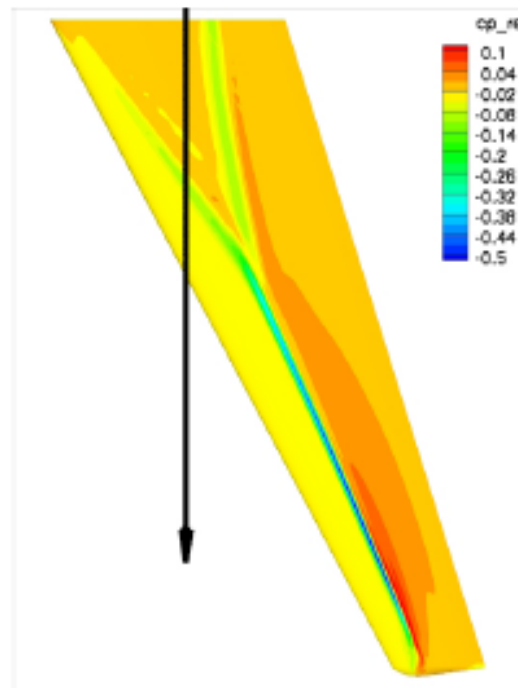
# LFD – RANS TAU Validation

LANN wing CT5,  $Ma=0.82$ ,  $Re=7.5$  mio,  $\alpha=0.6^\circ$ ,  $\Delta\alpha=0.25^\circ$ ,  $\omega^*=0.204$ , pitch

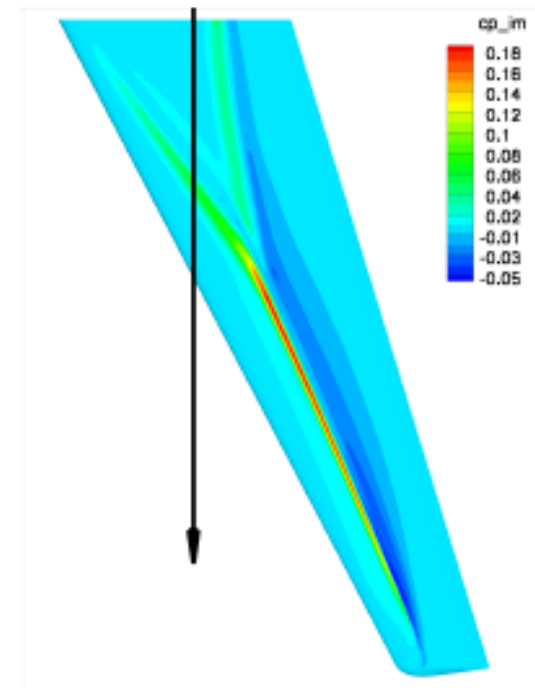
$C_p$  contour on upper surface of LANN wing CT5



(a)  $C_p^{mean}$

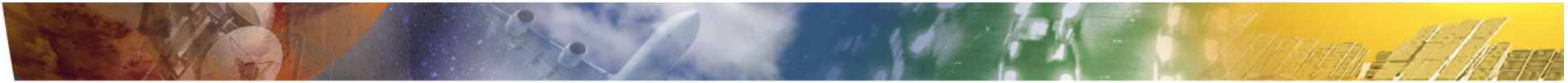


(b)  $C_p^{real}$

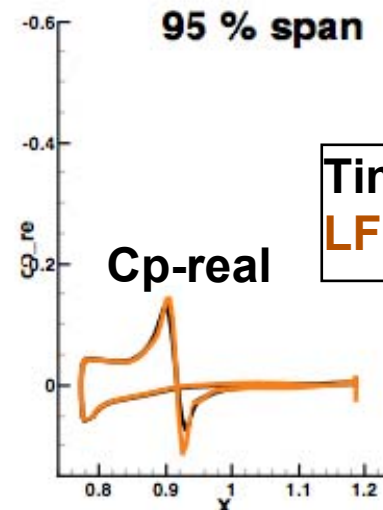
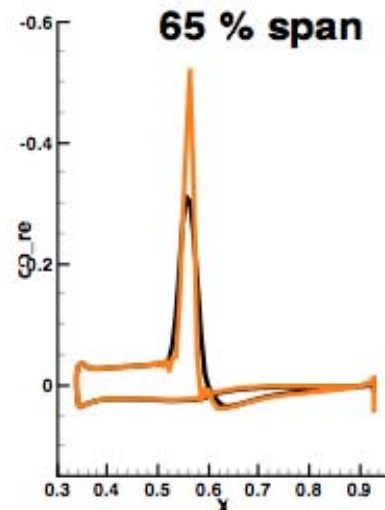
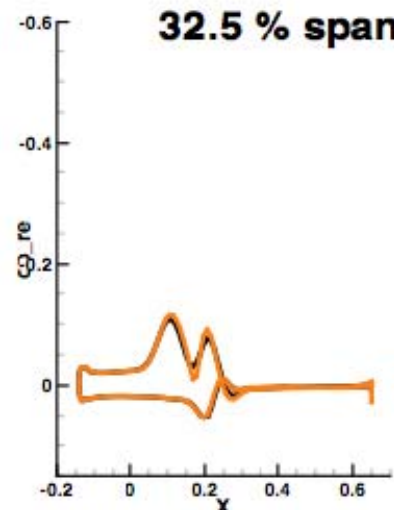


(c)  $C_p^{imag}$

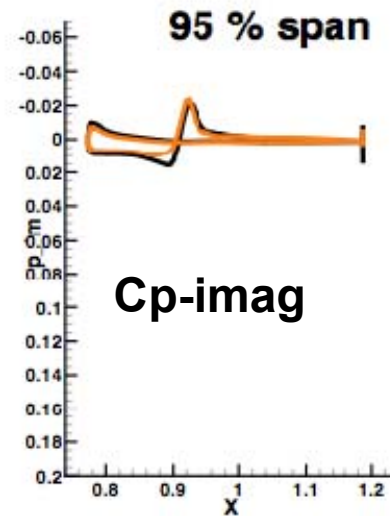
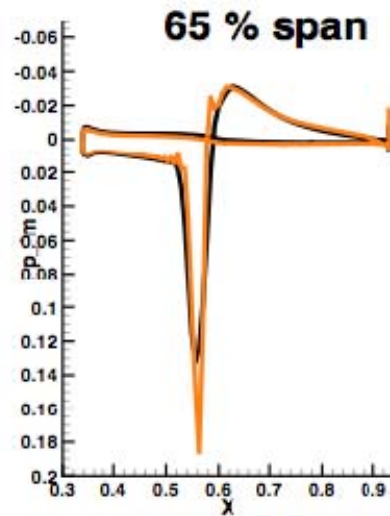
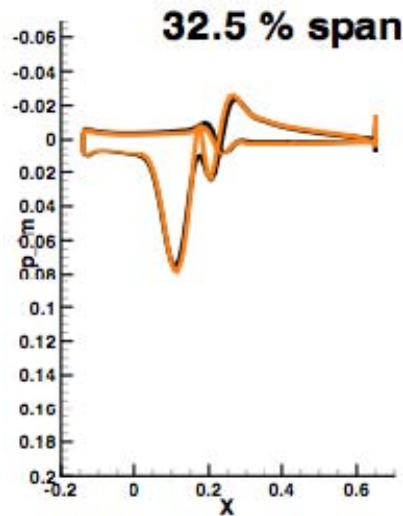




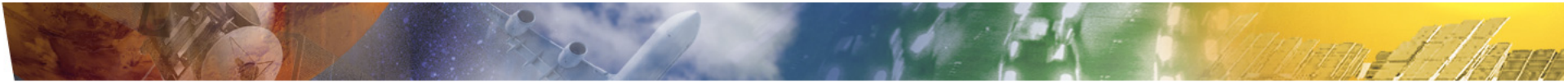
# LFD – RANS TAU Validation First Harmonic of Cp: LANN wing CT5



Time domain nonlinear  
**LFD**







# POD – Proper Orthogonal Decomposition

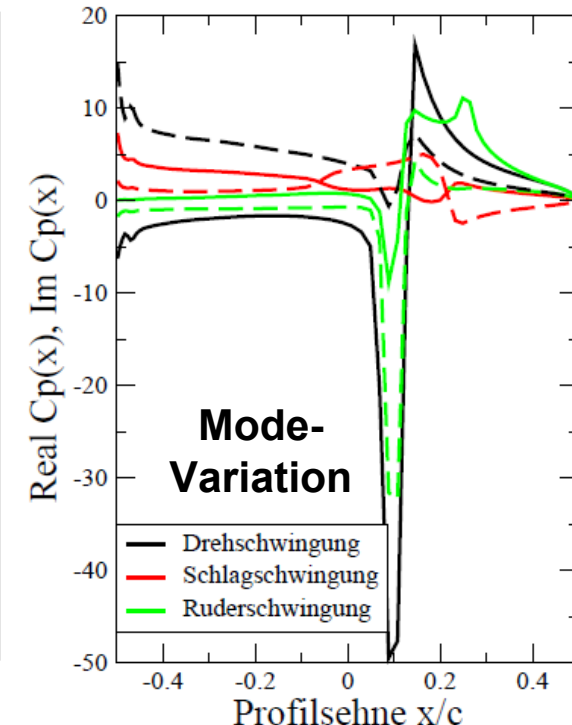
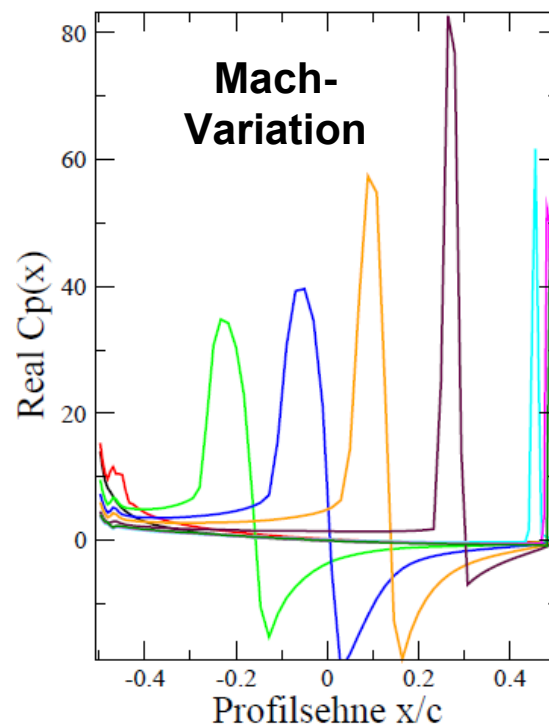
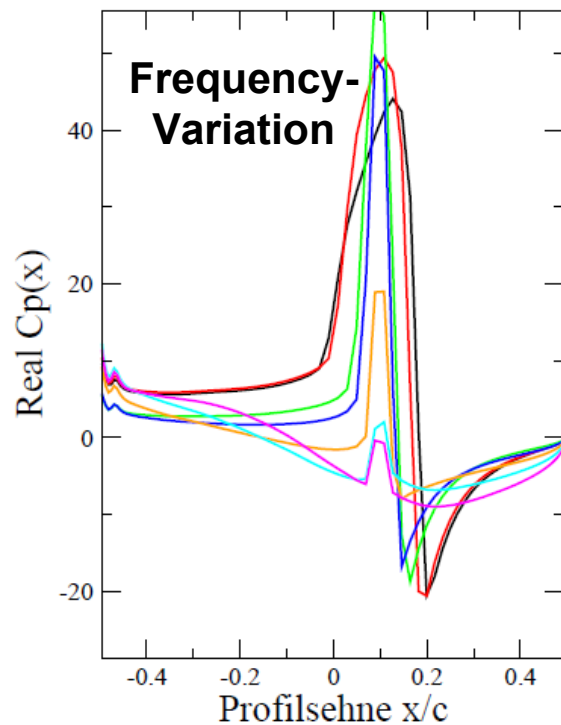
**Objective: Generate an optimal basis of small order for a manifold of required CFD results.**

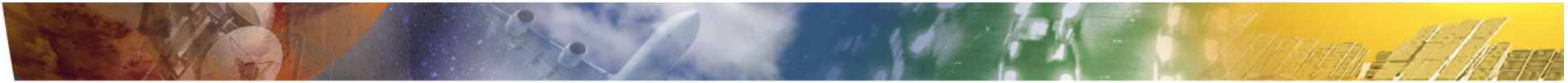
Computation of solutions (**snapshots**) for:

- 1. harmonic of unsteady flow fields
- 1. harmonic of surface  $C_p$  distribution
- Several parameter combinations (flow solutions for varying frequency, oscillation mode, Mach number, AoA, ..., → **N snapshots**)
- Fill these solution vectors in columns of a matrix → Snapshot-Matrix  $S$
- Compute Eigenvalues and Eigenvectors of the symmetric  $W=S^T S$
- Take those  $p$  Eigenvectors  $V$ , whose Eigenvalues have the biggest magnitude →  $p$  vectors  $V$
- → POD-Basis  $\Phi = SV$
- The  $N$  snapshot solutions and even more can be approximated by superposition of  $p$  POD basis vectors:  $S_i = \Phi w_i$

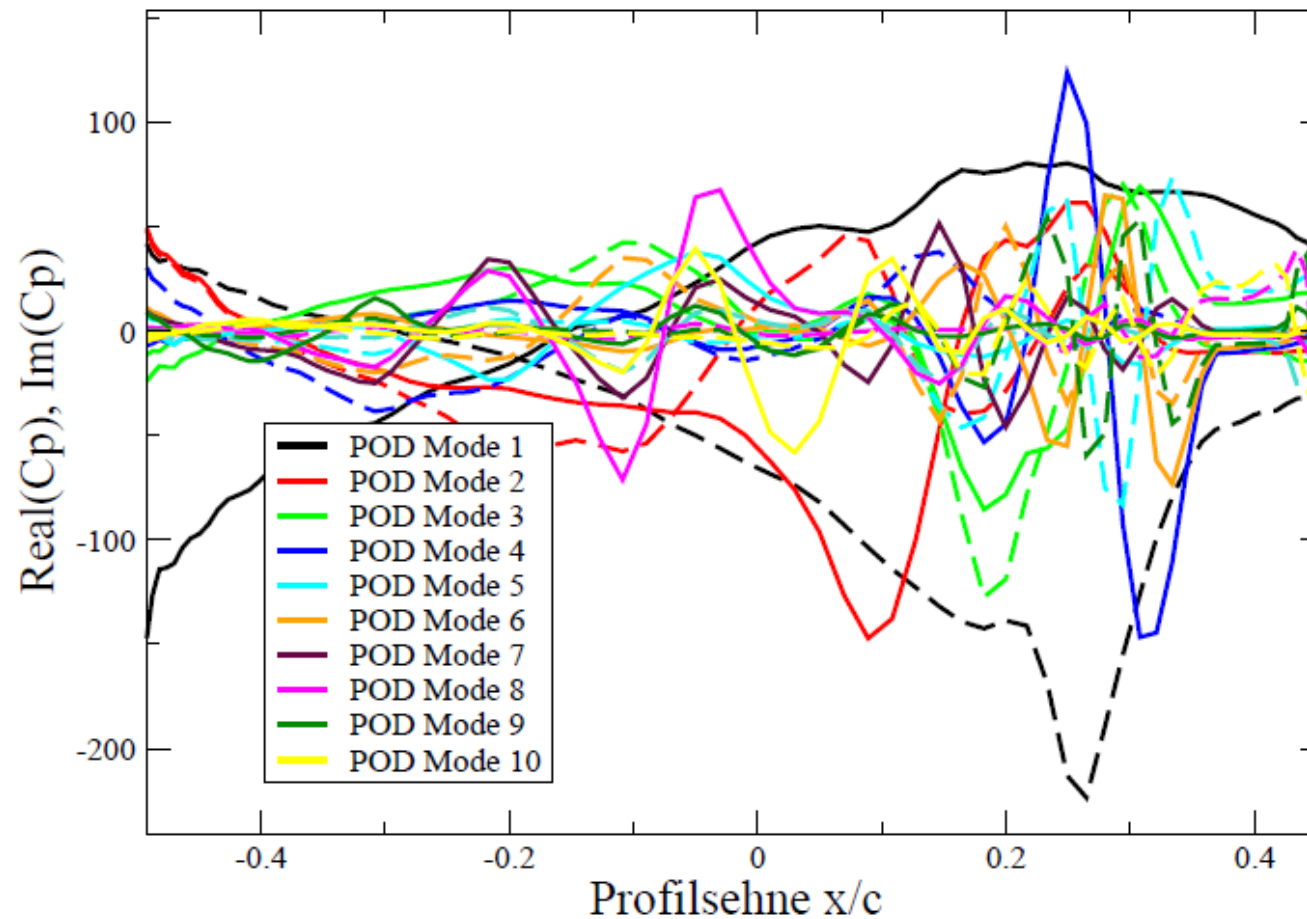
# POD – Example: Snapshots of 2D Oscillating Airfoil

- Unsteady surface pressure Cp-distribution (Real- und Imag.)
- NLR7301-airfoil, variation of:  $Ma$ ,  $\alpha$ ,  $\omega^*$ , oscill. Modes (9, 7, 5, 3)
- 945 simulations (Snapshots)

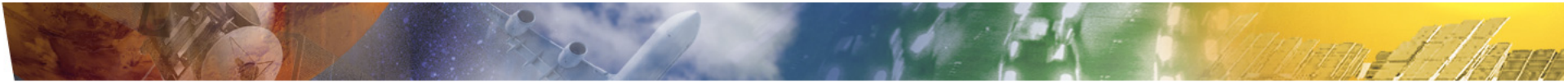




# The first 10 POD Modes seem to have no physical meaning



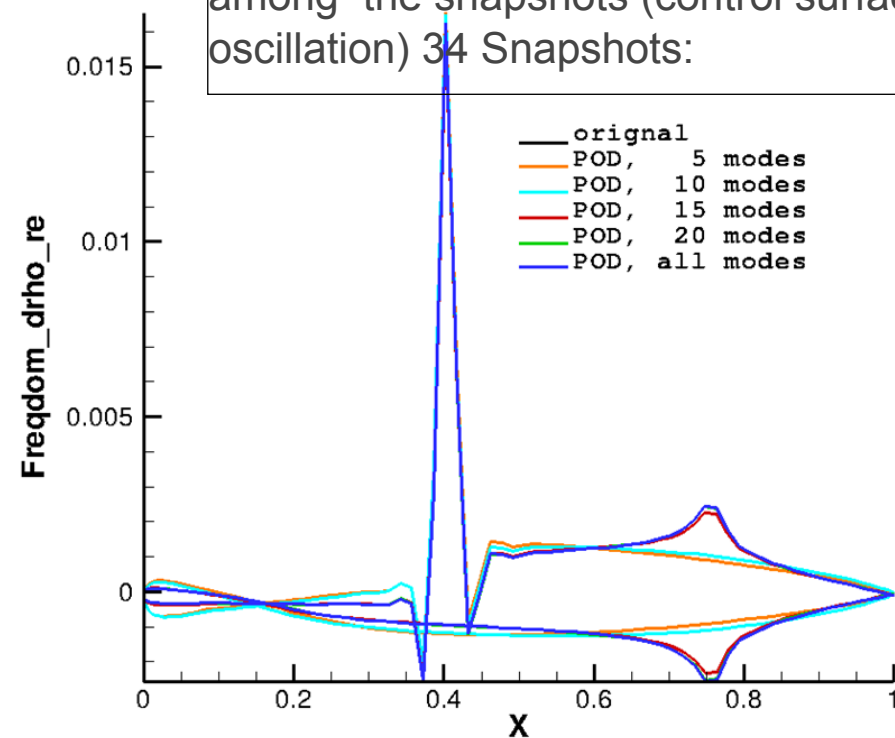
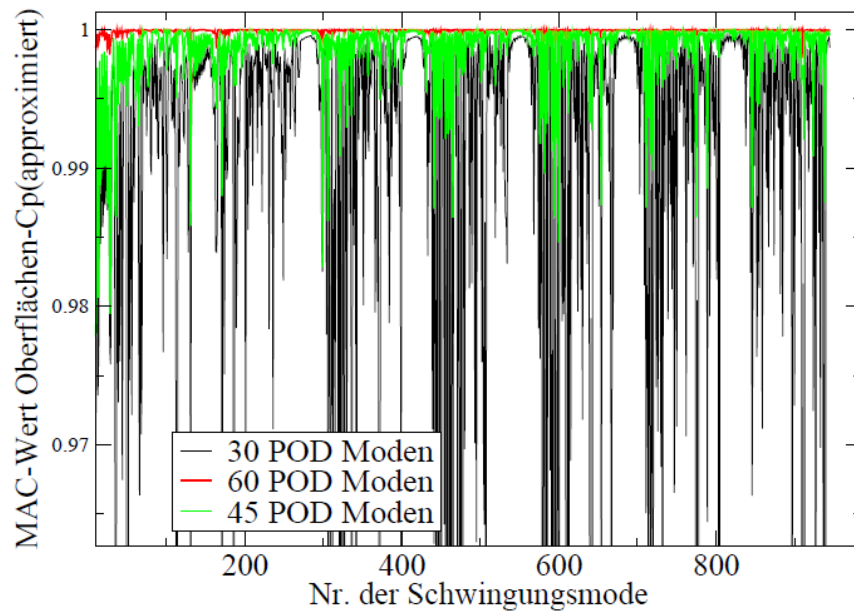


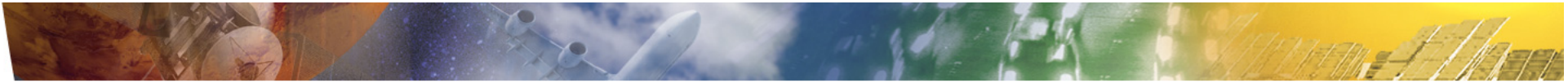


# POD

- A reduced POD Basis of vectors  $C_p(x)$  can be derived, all snapshots can be reconstructed by linear superposition.
- Only 45 POD modes sufficient to construct all 945 Snapshots → reduction of computational effort by factor of 20 ?
- But: POD modes without physical meaning
- Problem: proper choice of snapshots

Other example: case, which was not among the snapshots (control surface oscillation) 34 Snapshots:





## Conclusion

- **Unsteady CFD methods (RANS) are well validated by windtunnel tests**
- **for aeroelastic applications CPU effort has to be reduced significantly**
- **Different methods are developed and tested**
- **A combination of several methods is promising (factor 1000)**